Visit

FREETESTPAPER.com

for more papers



Website: freetestpaper.com



Facebook.com/freetestpaper



Twitter.com/freetestpaper

Name:	Class:	Class Register Number:

中正中学

CHUNG CHENG HIGH SCHOOL (MAIN)

Chung Cheng High School Chung Cheng High School Chung Cheng High School Chung Cheng High School Chung Cheng High School
Chung Cheng High School Chung Cheng High School Chung Cheng High School Chung Cheng High School Chung Cheng High School
Chung Cheng High School Chung Cheng High School Chung Cheng High School Chung Cheng High School Chung Cheng High School
Chung Cheng High School Chung Cheng High School Chung Cheng High School Chung Cheng High School Chung Cheng High School
Chung Cheng High School Chung Cheng High School Chung Cheng High School Chung Cheng High School Chung Cheng High School

Parent's Signature

PRELIMINARY EXAMINATION 2021
SECONDARY 4

MATHEMATICS 4048/01

Paper 1 **Wednesday 15 September 2021**

2 hours

Candidates answer on the Question Paper.

READ THESE INSTRUCTIONS FIRST

Write your name, class and index number on **all** the work you hand in.
Write in dark blue or black pen.
You may use an HB pencil for any diagrams or graphs.
Do not use staples, paper clips, glue or correction fluid.

Answer **all** questions.
If working is needed for any question it must be shown with the answer.
Omission of essential working will result in loss of marks.
The use of an approved scientific calculator is expected, where appropriate.
If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.
For π, use either your calculator value or 3.142, unless the question requires the answer in terms of π.

At the end of the examination, fasten all your work securely together.
The number of marks is given in brackets [ ] at the end of each question or part question.

The total number of marks for this paper is 80.

For Examiner's Use	
Total	**/ 80**

This document consists of **19** printed pages and **1** blank page.

[Turn over

FREE TEST PAPERS - FREETESTPAPER.COM

Mathematical Formulae

Compound interest

$$\text{Total amount} = P\left(1+\frac{r}{100}\right)^n$$

Mensuration

$$\text{Curved surface area of a cone} = \pi r l$$

$$\text{Surface area of a sphere} = 4\pi r^2$$

$$\text{Volume of a cone} = \frac{1}{3}\pi r^2 h$$

$$\text{Volume of a sphere} = \frac{4}{3}\pi r^3$$

$$\text{Area of triangle } ABC = \frac{1}{2}ab\sin C$$

$$\text{Arc length} = r\theta \text{, where } \theta \text{ is in radians}$$

$$\text{Sector area} = \frac{1}{2}r^2\theta \text{, where } \theta \text{ is in radians}$$

Trigonometry

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc\cos A$$

Statistics

$$\text{Mean} = \frac{\sum fx}{\sum f}$$

$$\text{Standard deviation} = \sqrt{\frac{\sum fx^2}{\sum f} - \left(\frac{\sum fx}{\sum f}\right)^2}$$

FREE TEST PAPERS - FREETESTPAPER.COM

Answer **all** the questions.

1 State which of the following number(s) is/are irrational.

$$0.\dot{5},\ \frac{\pi}{2},\ 2\sqrt{2},\ 3\sqrt{3}\times\sqrt{3}$$

Answer ..... [1]

---

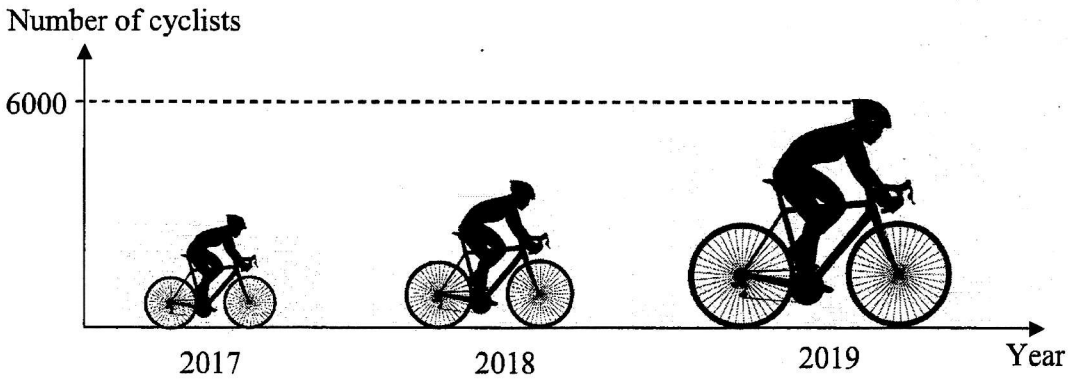
2 x is an integer greater than 1.
Write the following in order of size, starting with the largest.

$$x^0,\ x^{-\frac{3}{2}},\ x^{\frac{3}{4}},\ x^{\frac{3}{2}}$$

Answer ..... [1]

---

3 The graph shows the number of cyclists in an annual cycling marathon for the years 2017 to 2019.



(a) State one aspect of the graph that may be misleading.

.....

.....[1]

(b) Explain how this may lead to a misinterpretation of the graph.

.....

.....[1]

FREE TEST PAPERS - FREETESTPAPER.COM

4 **(a)** Simplify $\left(\frac{2^{a-1}\sqrt{2}}{2^a}\right)^2$.

Answer ..... [2]

(b) If $27m^{3x} = 1$ and $m > 0$, find $m^{2x} + m^{-x}$.

Answer ..... [2]

---

5 n is a positive integer.

Show that, for all n, $(5n+3)^2 - (5n-3)^2$ is a multiple of 4.

.....

.....

.....

.....

.....

.....

.....[2]

FREE TEST PAPERS - FREETESTPAPER.COM

6 Gladys wrote down four numbers.
The mean of these numbers is 13, the median is 12 and the mode is 10.
Find the four numbers.

Answer ..... [2]

---

7 **(a)** Mrs Boey deposited $20 000 in a bank that pays 0.8% per annum compound interest compounded half-yearly. Find the total amount of money she will receive at the end of 5 years, leaving your answer to the nearest cent.

Answer ..... [2]

(b)

> Singapore Budget 2018: GST to be raised from 7% to 9% some time between 2021 and 2025

Shane and Glen came across an article in the newspaper with the headline shown above and made the following comments.
Shane: Oh no, the GST will increase **by** 2% soon!
Glen: No! I disagree. It did not increase by 2%, in fact it is **MORE** than 2%!

Whose statement is correct? Support your answer with mathematical calculations.

Answer ..... [2]

FREE TEST PAPERS - FREETESTPAPER.COM

8 **(a)** Find the range of values of x which satisfy the inequalities

$$\frac{17-8x}{3} < \frac{2(3x-1)}{5} \leq 4.$$

Answer ..... [3]

(b) Hence, state the smallest prime number that satisfies the inequalities.

Answer ..... [1]

---

9 **(a)** Factorise completely $9b^2-6ab+a^2-x^2$.

Answer ..... [2]

(b) Simplify $\frac{5}{2x^2-7x-4} - \frac{8}{4-x}$.

Answer ..... [3]

FREE TEST PAPERS - FREETESTPAPER.COM

10 Roy made a model of his yacht with a scale of 1: 40.

(a) The actual length of the yacht is 12.5 m, find the length of the model in cm.

Answer .....cm [1]

(b) Roy wants to spray paint his yacht. He can select either of the following options to paint his yacht.

Option A: A lump sum payment of $1 000
Option B: Payment for cost of paint at $5.50 per m^2
[Cost of manpower is included in both options]

If the total surface area of the model to be painted is 937.5 cm^2, find the surface area of his yacht. Which one of the two options should Roy select to paint his yacht?
[Show your workings clearly]

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....[3]

FREE TEST PAPERS - FREETESTPAPER.COM

11 $\xi = \{x : x \text{ is an integer and } 1 \leq x \leq 10\}$

$A = \{x : x \text{ is a factor of } 20\}$

$B = \{x : x \text{ is a perfect square}\}$

Find

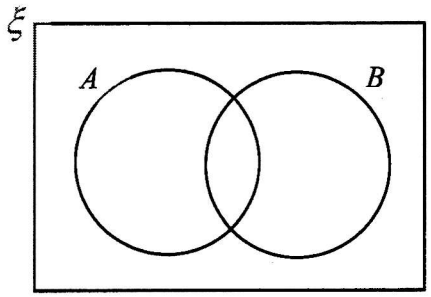
(a) $n(B)$,

Answer ..... [1]

(b) $A' \cap B'$.

Answer ..... [1]

(c) On the Venn Diagram, shade the region which represents $(A \cup B)' \cup (A \cap B)$.



[1]

FREE TEST PAPERS - FREETESTPAPER.COM

12 When written as the product of their prime factors,

p is $2^2 \times 3 \times 5$,

q is $2^6 \times 3^3$,

r is $2^2 \times 3^2 \times 11$.

Find

(a) the value of the cube root of q,

Answer ..... [1]

(b) the LCM of p, q and r, giving your answer as the product of its prime factors,

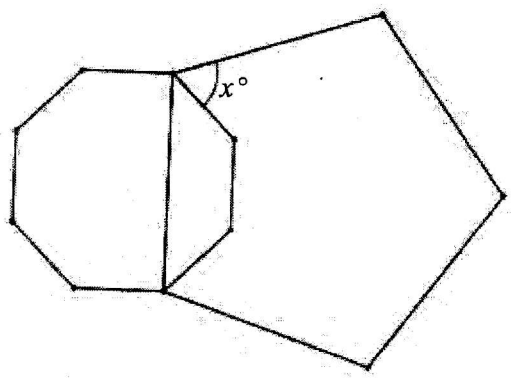
Answer ..... [1]

(c) the greatest number that will divide p, q and r exactly.

Answer ..... [1]

---

13 The diagram shows a regular pentagon and a regular octagon. Calculate the value of x.

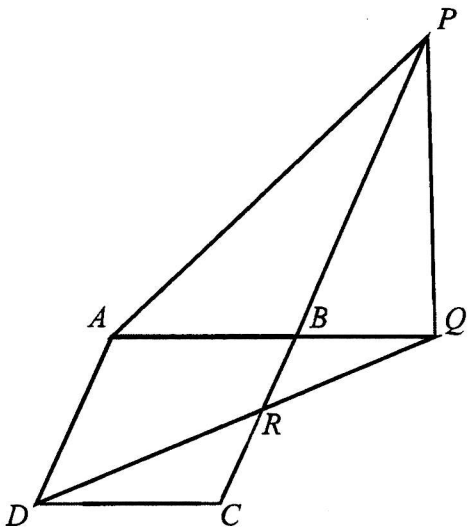


Answer $x =$ ..... [3]

FREE TEST PAPERS - FREETESTPAPER.COM

14 The diagram shows a rhombus $ABCD$.

ABQ, PBC and DRQ are straight lines and $AQ = BP$.



(a) State the triangle that is similar to triangle BRQ.

Answer Triangle ..... [1]

(b) Prove that triangle DQA is congruent to triangle APB.

.....

.....

.....

.....

.....

.....

.....

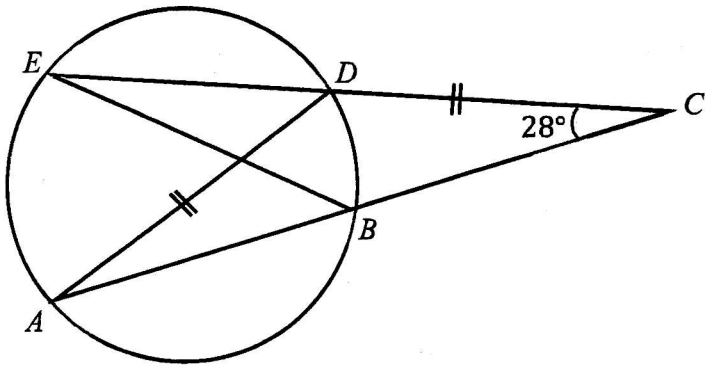
.....

.....

.....[2]

FREE TEST PAPERS - FREETESTPAPER.COM

15



A, B, D and E are points on the circle such that $AD = CD$ and angle $BCD = 28°$.
Explain with geometrical reasons, why the length of BC equals to BE.

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....[3]

FREE TEST PAPERS - FREETESTPAPER.COM

16 The masses of 20 bags, in kg, are measured.
The results are shown on the stem-and-leaf diagram.

Mass of 20 bags

Stem	Leaf
0	9
1	2
2	0 6 6 6
3	0 3 3 4 4 8 8
4	1 2 9 9 9
5	0 1

Key: 0|9 means 0.9 kg

(a) Find the mean mass of the bags.

Answer .....kg [1]

(b) Find the standard deviation of the masses of the bags.

Answer .....kg [1]

(c) It was found later that the weighing machine has an error.
Each bag was actually 0.08 kg heavier.
Explain how this will affect the mean and standard deviation.

.....

.....

.....

.....

.....[2]

FREE TEST PAPERS - FREETESTPAPER.COM

17 y is inversely proportional to the square of x, $x > 0$.

(a) If x is increased by 25%, find the percentage change in y.

Answer .....% [2]

(b) Given that $y = 16$ when $x = \frac{1}{2}$, find

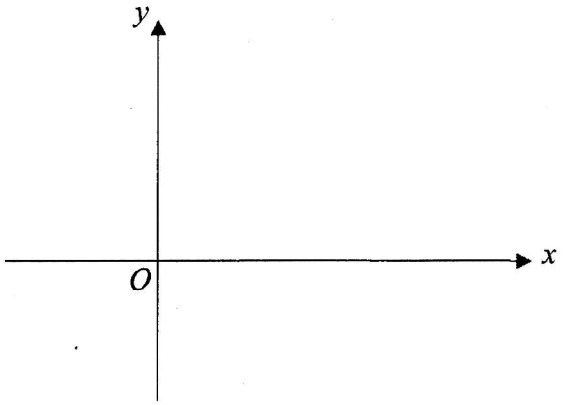
(i) the equation connecting y and x,

Answer ..... [2]

(ii) the value of x when $y = 100$.

Answer $x =$..... [2]

(c) Sketch the graph which represents the relation between y and x.



[1]

FREE TEST PAPERS - FREETESTPAPER.COM

18 In the following sequence,

$$(1\times 2)-2=0$$
$$(2\times 3)-4=2$$
$$(3\times 4)-6=6$$
$$(4\times 5)-8=12$$
.....
.....
$$(a\times 12)-b=c$$
.....
.....
$$(d\times e)-f=g$$

(a) Find the values of a, b and c.

Answer a =....., b = ..., c =..... [2]

(b) Express g in terms of d.

Answer ..... [2]

(c) Explain why 279 cannot be the result of an equation in this sequence.

.....

.....

.....

.....

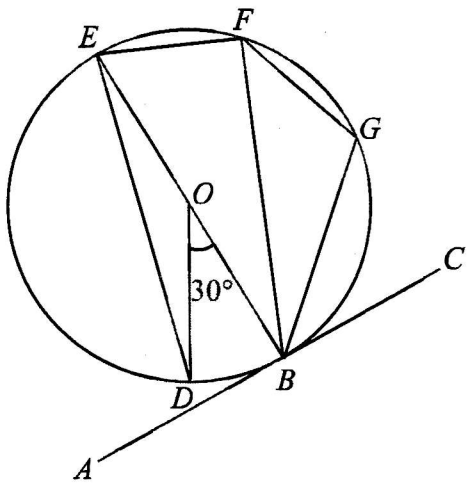
.....

.....

.....[1]

FREE TEST PAPERS - FREETESTPAPER.COM

19 The diagram shows a circle *BDEFG*, centre *O* and diameter *BE*. The line *AC* is a tangent to the circle at *B* and angle $BOD = 30°$. The ratio of angle *EBF* to angle *FBG* to angle *GBC* is 1 : 1 : 2.



(a) State a fact about the arcs *EF* and *FG*.

.....

.....[1]

(b) Showing all reasons clearly, find

(i) angle *DEB*,

Answer ..... [1]

(ii) angle *EFG*.

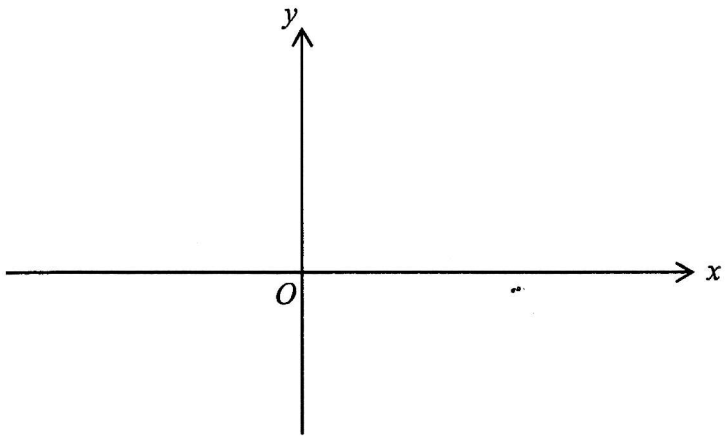
Answer ..... [2]

FREE TEST PAPERS - FREETESTPAPER.COM

20 **(a)** Express $-x^2+4x+12$ in the form $-(x+p)(x-q)$.

Answer ..... [1]

(b) Sketch the graph of $y=-x^2+4x+12$ on the axes below.
Indicate clearly the values where the graph crosses both axes. [2]



(c) Find the coordinates of the turning point.

Answer (....., ...) [1]

(d) Without solving the equation algebraically, explain why $-x^2+4x+12=18$ has no solution.

.....

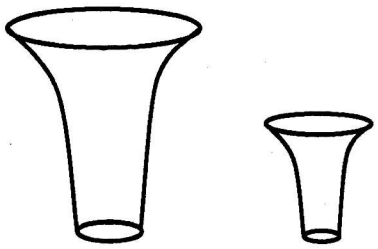
.....

.....

.....[1]

FREE TEST PAPERS - FREETESTPAPER.COM

21 The diagram shows two geometrically similar containers. The cost of painting the base area of the smaller container is $\frac{25}{64}$ of the cost of painting the base of the larger container.



(a) The top of the larger container has a circumference of 24 cm.
Find the circumference of the top of the smaller container.

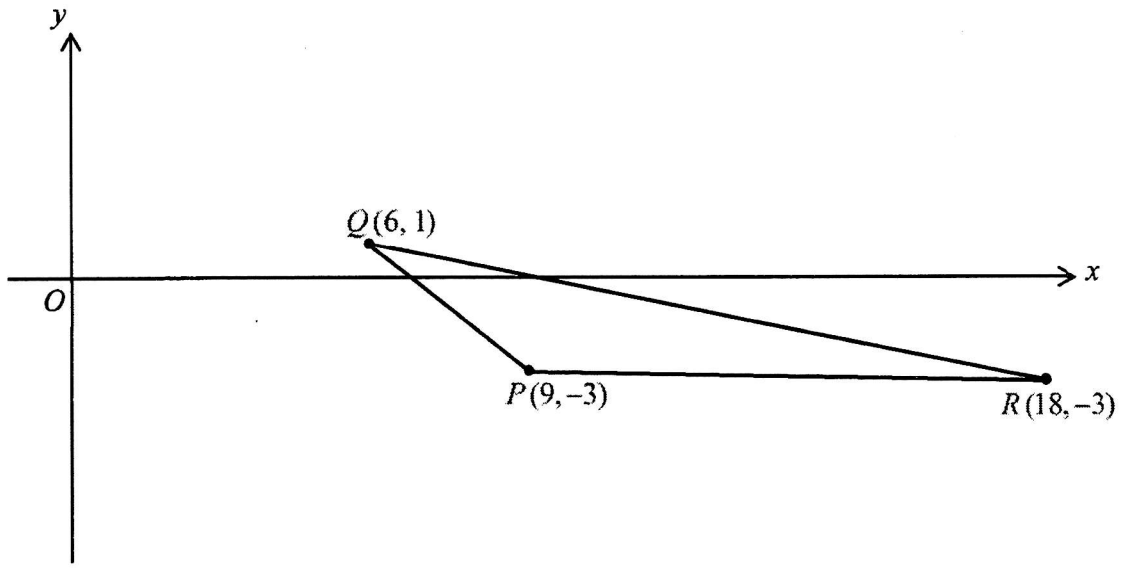
Answer ..... cm [2]

(b) The capacity of the smaller container is 0.45 litres.
Find the capacity of the larger container, giving your answer to 2 decimal places.

Answer ..... litres [1]

FREE TEST PAPERS - FREETESTPAPER.COM

22



In the diagram, the points P, Q and R have coordinates $(9,-3)$, $(6,1)$ and $(18,-3)$ respectively.

(a) Find the length of PQ.

Answer .....units [1]

(b) Find the value of $\cos \angle QPR$, giving your answer as a fraction in its simplest form.

Answer ..... [1]

(c) Find the area of triangle PQR.

Answer .....units^2 [1]

FREE TEST PAPERS - FREETESTPAPER.COM

(d) Find the equation of the line PQ.

Answer ..... [2]

(e) The equation of a line passing through the point R is $4x + 21y = 9$.

Find the coordinates of the point of intersection of this line and the line PQ.

Answer ..... [3]

~ End of Paper ~

FREE TEST PAPERS - FREETESTPAPER.COM

BLANK PAGE

FREE TEST PAPERS - FREETESTPAPER.COM

ANS

Name:	Class:	SOLUTIONS

中正中学

CHUNG CHENG HIGH SCHOOL (MAIN)

Chung Cheng High School Chung Cheng High School Chung Cheng High School Chung Cheng High School Chung Cheng High School
Chung Cheng High School Chung Cheng High School Chung Cheng High School Chung Cheng High School Chung Cheng High School
Chung Cheng High School Chung Cheng High School Chung Cheng High School Chung Cheng High School Chung Cheng High School
Chung Cheng High School Chung Cheng High School Chung Cheng High School Chung Cheng High School Chung Cheng High School
Chung Cheng High School Chung Cheng High School Chung Cheng High School Chung Cheng High School Chung Cheng High School

Parent's Signature

PRELIMINARY EXAMINATION 2021
SECONDARY 4

MATHEMATICS **4048/01**

Paper 1 **Wednesday 15 September 2021**

2 hours

Candidates answer on the Question Paper.

READ THESE INSTRUCTIONS FIRST

Write your name, class and index number on all the work you hand in.
Write in dark blue or black pen.
You may use an HB pencil for any diagrams or graphs.
Do not use staples, paper clips, glue or correction fluid.

Answer **all** questions.
If working is needed for any question it must be shown with the answer.
Omission of essential working will result in loss of marks.
The use of an approved scientific calculator is expected, where appropriate.
If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.
For π, use either your calculator value or 3.142, unless the question requires the answer in terms of π.

At the end of the examination, fasten all your work securely together.
The number of marks is given in brackets [ ] at the end of each question or part question.

The total number of marks for this paper is 80.

For Examiner's Use	
Total	**/ 80**

This document consists of **19** printed pages and **1** blank page.

[Turn over

FREE TEST PAPERS - FREETESTPAPER.COM

Mathematical Formulae

Compound interest

$$\text{Total amount} = P\left(1+\frac{r}{100}\right)^n$$

Mensuration

$$\text{Curved surface area of a cone} = \pi r l$$

$$\text{Surface area of a sphere} = 4\pi r^2$$

$$\text{Volume of a cone} = \frac{1}{3}\pi r^2 h$$

$$\text{Volume of a sphere} = \frac{4}{3}\pi r^3$$

$$\text{Area of triangle } ABC = \frac{1}{2}ab\sin C$$

$$\text{Arc length} = r\theta \text{ , where } \theta \text{ is in radians}$$

$$\text{Sector area} = \frac{1}{2}r^2\theta \text{ , where } \theta \text{ is in radians}$$

Trigonometry

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc\cos A$$

Statistics

$$\text{Mean} = \frac{\Sigma fx}{\Sigma f}$$

$$\text{Standard deviation} = \sqrt{\frac{\Sigma fx^2}{\Sigma f} - \left(\frac{\Sigma fx}{\Sigma f}\right)^2}$$

FREE TEST PAPERS - FREETESTPAPER.COM

Answer **all** the questions.

1 State which of the following number(s) is/are irrational.

$0.\dot{5}$, $\frac{\pi}{2}$, $2\sqrt{2}$, $3\sqrt{3}\times\sqrt{3}$

$\frac{\pi}{2}$, $2\sqrt{2}$

$0.\dot{5}$ can be expressed as $\frac{5}{9}$, so $0.\dot{5}$ is a rational number

Answer ..... [1]

---

2 x is an integer greater than 1.
Write the following in order of size, starting with the largest.

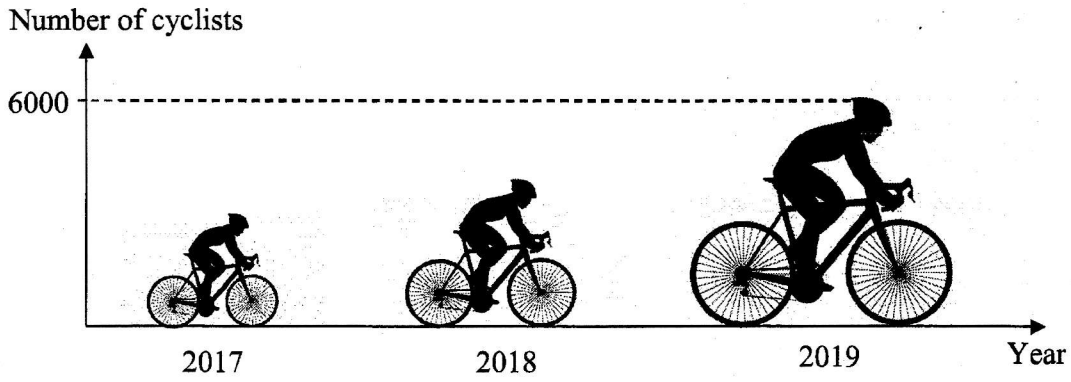
x^0, $x^{-\frac{3}{2}}$, $x^{\frac{3}{4}}$, $x^{\frac{3}{2}}$

$x^{\frac{3}{2}}$, $x^{\frac{3}{4}}$, x^0, $x^{-\frac{3}{2}}$

Answer ..... [1]

---

3 The graph shows the number of cyclists in an annual cycling marathon for the years 2017 to 2019.



(a) State one aspect of the graph that may be misleading.

The vertical axis is not labelled at the start / No "0" on the y-axis. **OR**

The size of the picture not only increases with height, but also in the width.

(b) Explain how this may lead to a misinterpretation of the graph.

It is difficult to estimate the number of cyclists for 2017 and 2018. **OR**

Unclear as to whether the height or the area is used to determine the number of cyclists

FREE TEST PAPERS - FREETESTPAPER.COM

4 **(a)** Simplify $\left(\frac{2^{a-1}\sqrt{2}}{2^a}\right)^2$.

$$\left(\frac{2^{a-1}\sqrt{2}}{2^a}\right)^2 = \left(\frac{2^a.2^{-1}.\sqrt{2}}{2^a}\right)^2$$

$$= \left(\frac{\sqrt{2}}{2}\right)^2$$

$$= \frac{2}{4}$$

$$= \frac{1}{2}$$

2^{-1} is considered as not simplified, need to simplify to $\frac{1}{2}$

Answer ..... [2]

(b) If $27m^{3x} = 1$ and $m > 0$, find $m^{2x} + m^{-x}$.

$$27m^{3x} = 1$$

$$m^{3x} = \frac{1}{27}$$

$$m^x = \frac{1}{3}$$

$$m^{2x} + m^{-x} = \left(m^x\right)^2 + \left(m^x\right)^{-1}$$

$$= \left(\frac{1}{3}\right)^2 + \left(\frac{1}{3}\right)^{-1}$$

$$= 3\frac{1}{9}$$

Some obtained $m^{3x} = 3^{-3}$ and from this step, some went to equate m = 3 and $x = -1$ which is not always true as $m = \frac{1}{3}, x = 1$ *or* $m = 9, x = -\frac{1}{2}$.
As there are 2 unknown variables in this equation so we need two equations to be solved simultaneously in order to solve for the value of m and x.

Answer ..... [2]

---

5 n is a positive integer.

Show that, for all n, $(5n+3)^2 - (5n-3)^2$ is a multiple of 4. [2]

Answer

$$(5n+3)^2 - (5n-3)^2 = (5n+3+5n-3)(5n+3-(5n-3))$$

$$= (10n)(6)$$

$$= 60n$$

$$= 4(15n)$$

Since n is a positive integer and $60n = 4(15n)$, $(5n+3)^2 - (5n-3)^2$ is a multiple of 4.

FREE TEST PAPERS - FREETESTPAPER.COM

6 Gladys wrote down four numbers.
The mean of these numbers is 13, the median is 12 and the mode is 10.
Find the four numbers.

Let the four numbers be a, b, c and d in ascending order.
Since the mode is smaller than the median, a and b will be 10.
Since median is 12,

$$\frac{10+c}{2}=12$$
$$c=24-10$$
$$=14$$

Since mean is 13,

$$10+10+14+d=13\times4$$
$$d=18$$

The four numbers are 10, 10, 14 and 18.

Answer ..... [2]

---

7 **(a)** Mrs Boey deposited \$20 000 in a bank that pays 0.8% per annum compound interest compounded half-yearly. Find the total amount of money she will receive at the end of 5 years, leaving your answer to the nearest cent.

$$\text{Total amount} = \$20000\left(1+\frac{0.8}{2(100)}\right)^{5\times2}$$
$$=\$20814.55468$$
$$=\$20814.55 \text{ (nearest cent)}$$

Answer ..... [2]

(b)

> Singapore Budget 2018: GST to be raised from 7% to 9% some time between 2021 and 2025

Shane and Glen came across an article in the newspaper with the headline shown above and made the following comments.
Shane: Oh no, the GST will increase **by** 2% soon!
Glen: No! I disagree. It did not increase by 2%, in fact it is **MORE** than 2%!

Whose statement is correct? Support your answer with mathematical calculations.

$$\frac{9-7}{7}\times100\% = 28.6\%\,(3sf)$$

> **Percentage point** is defined as the **difference** between two percentages. So the increase from 7% to 9% is two percentage points, and not two percent.

Glen's statement is correct as the GST will increase by 28.6%, which is more than 2%.

Answer ..... [2]

FREE TEST PAPERS - FREETESTPAPER.COM

8 **(a)** Find the range of values of x which satisfy the inequalities

$$\frac{17-8x}{3} < \frac{2(3x-1)}{5} \leq 4.$$

$$\frac{2(3x-1)}{5} \leq 4$$
$$3x-1 \leq 10$$
$$3x \leq 11$$
$$x \leq 3\frac{2}{3}$$

and

$$\frac{17-8x}{3} < \frac{2(3x-1)}{5}$$
$$5(17-8x) < 6(3x-1)$$
$$85-40x < 18x-6$$
$$-58x < -91$$
$$x > \frac{91}{58}$$
$$x > 1\frac{33}{58}$$

$$\therefore 1\frac{33}{58} < x \leq 3\frac{2}{3}$$

Answer ..... [3]

(b) Hence, state the smallest prime number that satisfies the inequalities.

Smallest prime number is 2.

Answer ..... [1]

---

9 **(a)** Factorise completely $9b^2-6ab+a^2-x^2$.

$$9b^2-6ab+a^2-x^2 = (3b-a)^2-x^2$$
$$= (3b-a+x)(3b-a-x)$$

Or

$$9b^2-6ab+a^2-x^2 = (a-3b)^2-x^2$$
$$= (a-3b+x)(a-3b-x)$$

Answer ..... [2]

(b) Simplify $\frac{5}{2x^2-7x-4} - \frac{8}{4-x}$.

$$\frac{5}{2x^2-7x-4} - \frac{8}{4-x} = \frac{5}{(2x+1)(x-4)} + \frac{8}{x-4}$$
$$= \frac{5+8(2x+1)}{(2x+1)(x-4)}$$
$$= \frac{5+16x+8}{(2x+1)(x-4)}$$
$$= \frac{16x+13}{(2x+1)(x-4)}$$

Answer ..... [3]

FREE TEST PAPERS - FREETESTPAPER.COM

10 Roy made a model of his yacht with a scale of 1: 40.

(a) The actual length of the yacht is 12.5 m, find the length of the model in cm.

1: 40
1 cm: 0.4 m

$$\text{Length of model} = \frac{12.5}{0.4}$$
$$= 31.25 \text{ cm}$$

The value 31.25 is exact, so it should not be expressed as 31.3 (correct to 3 s.f.)

Answer .....cm [1]

(b) Roy wants to spray paint his yacht. He can select either of the following options to paint his yacht.

Option A: A lump sum payment of \$1 000
Option B: Payment for cost of paint at \$5.50 per m^2
[Cost of manpower is included in both options]

If the total surface area of the model to be painted is 937.5 cm^2, find the surface area of his yacht. Which one of the two options should Roy select to paint his yacht?
[Show your workings clearly]

1 cm: 0.4 m
1 cm^2 : $(0.4)^2$ m^2
1 cm^2 : 0.16 m^2

$$\text{Cost of paint} = 937.5 \times 0.16 \times \$5.50$$
$$= \$825$$

Roy should select Option B as it is cheaper.

Answer .....

.....[3]

FREE TEST PAPERS - FREETESTPAPER.COM

11 $\xi = \{x : x \text{ is an integer and } 1 \leq x \leq 10\}$

$A = \{x : x \text{ is a factor of } 20\}$

$B = \{x : x \text{ is a perfect square}\}$

Find

(a) $n(B)$,

$\xi = \{1,\ 2,\ 3,\ 4,\ 5,\ 6,\ 7,\ 8,\ 9,\ 10\}$

$A = \{1,\ 2,\ 4,\ 5,\ 10\}$

$B = \{1,\ 4,\ 9\}$

** 1 is a perfect square

$n(B) = 3$

Answer ..... [1]

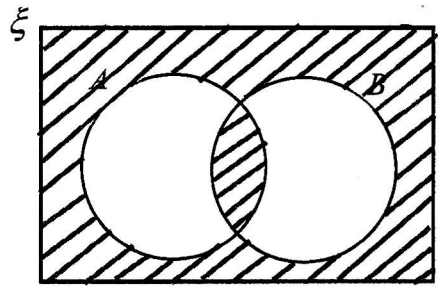
(b) $A' \cap B'$.

$A' \cap B' = \{3,\ 6,\ 7,\ 8\}$

It is a set, so curly brackets must be included.

Answer ..... [1]

(c) On the Venn Diagram, shade the region which represents $(A \cup B)' \cup (A \cap B)$.



[1]

FREE TEST PAPERS - FREETESTPAPER.COM

12 When written as the product of their prime factors,

p is $2^2 \times 3 \times 5$,

q is $2^6 \times 3^3$,

r is $2^2 \times 3^2 \times 11$.

Find

(a) the value of the cube root of q,

Cube root of $q = 2^2 \times 3$

$= 12$

Answer ..... [1]

(b) the LCM of p, q and r, giving your answer as the product of its prime factors,

LCM of p, q and $r = 2^6 \times 3^3 \times 5 \times 11$

Answer ..... [1]

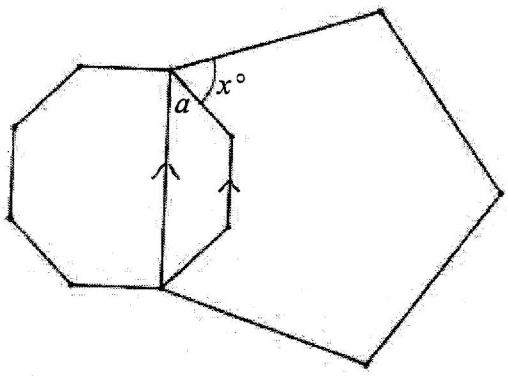
(c) the greatest number that will divide p, q and r exactly.

The greatest number = HCF $= 2^2 \times 3 = 12$

Answer ..... [1]

---

13 The diagram shows a regular pentagon and a regular octagon. Calculate the value of x.



Each interior angle of pentagon $= \frac{(5-2)}{5} \times 180°$

$= 108°$

Each interior angle of octagon $= \frac{(8-2)}{8} \times 180°$

$= 135°$

$a = \frac{1}{2}(360° - 2 \times 135°)$ ($\angle$ sum of isosceles trapezium)

$= 45°$

$x° = 108° - 45°$

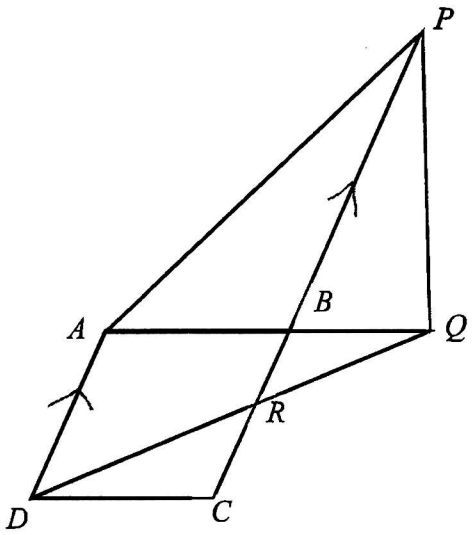
$= 63°$

Answer $x =$ ..... [3]

FREE TEST PAPERS - FREETESTPAPER.COM

14 The diagram shows a rhombus $ABCD$.

ABQ, PBC and DRQ are straight lines and $AQ = BP$.



(a) State the triangle that is similar to triangle BRQ.

Triangle ADQ or Triangle CRD

Answer Triangle ..... [1]

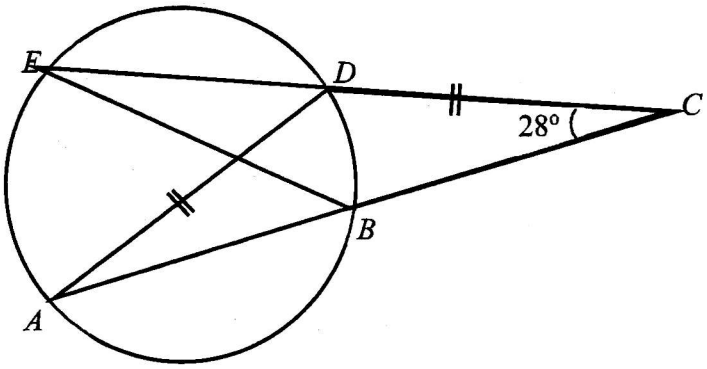
(b) Prove that triangle DQA is congruent to triangle APB.

$AD = AB$ (given $ABCD$ is a rhombus)
angle DAQ = angle ABP (alternate angles, AD parallel to BC and BP)
$AQ = BP$ (given)
Therefore triangle DQA is congruent to triangle APB. (SAS)

[2]

FREE TEST PAPERS - FREETESTPAPER.COM

15



A, B, D and E are points on the circle such that $AD = CD$ and angle $BCD = 28°$.
Explain with geometrical reasons, why the length of BC equals to BE.

Angle $DAC = 28°$ (base angles of isosceles triangle ACD)

Angle DEB = Angle DAC (angles in same segment)

$= 28°$

= Angle BCD

So triangle BCE is an isosceles triangle.

Therefore the length of BC equals to BE.

Many students are not able to spell the word **isosceles** correctly.

[3]

FREE TEST PAPERS - FREETESTPAPER.COM

16 The masses of 20 bags, in kg, are measured.
The results are shown on the stem-and-leaf diagram.

Mass of 20 bags

Stem	Leaf
0	9
1	2
2	0 6 6 6
3	0 3 3 4 4 8 8
4	1 2 9 9 9
5	0 1

Key: 0|9 means 0.9 kg

(a) Find the mean mass of the bags.

$$\text{Mean mass} = \frac{69}{20} \text{ kg}$$
$$= 3.45 \text{ kg}$$

A few forgot to check the key and did not realise the decimal point, hence giving the answer as 34.5 kg which is incorrect.

Answer .....kg [1]

(b) Find the standard deviation of the masses of the bags.

$$\text{Standard deviation} = \sqrt{\frac{266.8}{30} - 3.45^2} \text{ kg}$$
$$= 1.20 \text{ kg (3 s.f.)}$$

Answer .....kg [1]

(c) It was found later that the weighing machine has an error.
Each bag was actually 0.08 kg heavier.
Explain how this will affect the mean and standard deviation.

Answer
The mean will increase by 0.08 kg.
The standard deviation will remain the same.

[2]

---

17 y is inversely proportional to the square of x, $x > 0$.

FREE TEST PAPERS - FREETESTPAPER.COM

(a) If x is increased by 25%, find the percentage change in y.

$y = \frac{k}{x^2}$ where k is a constant

$$\text{New } y = \frac{k}{\left(\frac{125}{100}x\right)^2}$$

$$= \frac{16}{25}\left(\frac{k}{x^2}\right)$$

$$= \frac{16}{25}y$$

Quite a few missed the negative sign as it is a **decrease** in y.

$$\text{Percentage change} = \frac{new - original}{original} \times 100\%$$

$$\text{Percentage change in } y = \frac{\frac{16}{25}y - y}{y} \times 100\%$$

$$= -36\%$$

Answer .....% [2]

(b) Given that $y = 16$ when $x = \frac{1}{2}$, find

(i) the equation connecting y and x,

$$k = yx^2$$

$$= 16\left(\frac{1}{2}\right)^2$$

$$= 4$$

$$\therefore y = \frac{4}{x^2}$$

Answer ..... [2]

(ii) the value of x when $y = 100$.

When $y = 100$,

$$x^2 = \frac{4}{100}$$

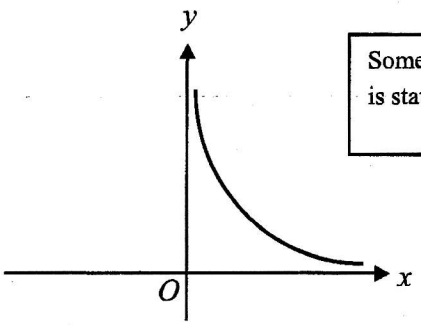
$$= \frac{1}{25}$$

$$x = \frac{1}{5}$$

Some forgot to reject the negative value as it is given at the beginning of the question that $x > 0$.

Answer $x =$..... [2]

(c) Sketch the graph which represents the relation between y and x. [1]



Some still include the negative part even though it is stated at the beginning of the question that $x > 0$.

---

18 In the following sequence,

FREE TEST PAPERS - FREETESTPAPER.COM

$(1\times2)-2=0$
$(2\times3)-4=2$
$(3\times4)-6=6$
$(4\times5)-8=12$
.....
.....
$(a\times12)-b=c$
.....
.....
$(d\times e)-f=g$

(a) Find the values of a, b and c.

$a=11$ $\quad b=2\times11$ $\quad c=11\times12-22$
$\quad\quad\quad =22$ $\quad\quad\quad =110$

Answer $a=$....., $b=$ ....., $c=$..... [2]

(b) Express g in terms of d.

$e=d+1$
$f=2d$

$g=d(d+1)-2d$
$g=d^2+d-2d$
$g=d^2-d$
$g=d(d-1)$

Some left out the " g = " part in their answer blank which is part of the required answer.

Answer ..... [2]

(c) Explain why 279 cannot be the result of an equation in this sequence.

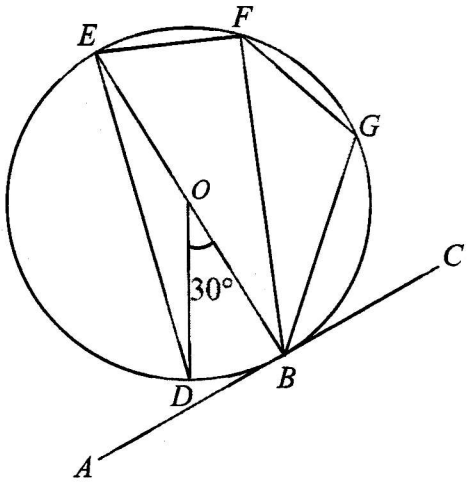
Answer ..... [1]

g is the product of an odd and an even number. Therefore g must be even. Since 279 is odd, 279 cannot be the result of an equation.

Alternatively,
$279=9\times31$
From **(b),** g is the product of 2 consecutive integers which is an even number.
279 is odd, therefore 279 cannot be the result of an equation in this sequence..

FREE TEST PAPERS - FREETESTPAPER.COM

19 The diagram shows a circle $BDEFG$, centre O and diameter BE. The line AC is a tangent to the circle at B and angle $BOD = 30°$. The ratio of angle EBF to angle FBG to angle GBC is 1 : 1 : 2.



(a) State a fact about the arcs EF and FG.

Answer Arc EF = Arc FG .....[1]

(b) Showing all reasons clearly, find

(i) angle DEB,

angle $DEB = 15°$ (angle at centre = 2 × angle at circumference)

Answer ..... [1]

(ii) angle EFG.

angle $EBC = 90°$ (tangent perpendicular to radius)

angle $EBG = \frac{2}{4} \times 90°$

$= 45°$

angle $EFG = 180° - 45°$ (angles in opposite segments)

$= 135°$

Some are still not using the standardised geometrical reasons/statements for stating the reasons.

Students must use only the given standardised geometrical properties/ reasons.

Some are using very long-winded methods even though it is only 2 marks.

Answer ..... [2]

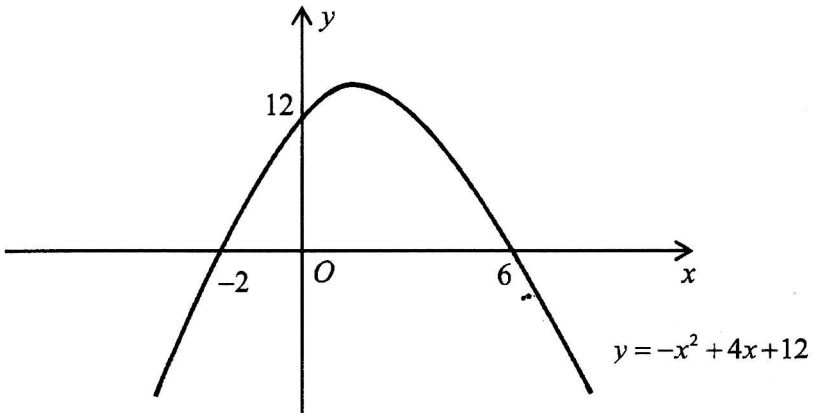
FREE TEST PAPERS - FREETESTPAPER.COM

20 **(a)** Express $-x^2+4x+12$ in the form $-(x+p)(x-q)$.

$$-x^2+4x+12=-(x^2-4x-12)$$
$$=-(x+2)(x-6)$$

Answer ..... [1]

(b) Sketch the graph of $y=-x^2+4x+12$ on the axes below.
Indicate clearly the values where the graph crosses both axes. [2]



(c) Find the coordinates of the turning point.

Turning point is (2, 16).

Answer (....., ...) [1]

(d) Without solving the equation algebraically, explain why $-x^2+4x+12=18$ has no solution.

Since the maximum value of the curve y is 16, there is no point of intersection between the curve and the horizontal straight line $y = 18$.

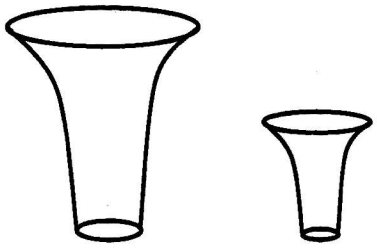
Or
The line $y = 18$ is always above the curve, so there is no point of intersection between the curve and the straight line $y = 18$.

Answer .....
.....[1]

Some are still using algebraic method to solve despite the instruction saying otherwise.

FREE TEST PAPERS - FREETESTPAPER.COM

21 The diagram shows two **geometrically similar** containers. The cost of painting the base **area** of the smaller container is $\frac{25}{64}$ of the cost of painting the base of the larger container.



(a) The top of the larger container has a circumference of 24 cm.
Find the circumference of the top of the smaller container.

$$\left(\frac{l_s}{l_l}\right) = \sqrt{\frac{25}{64}} = \frac{5}{8}$$

$$\text{Circumference of the top of smaller container} = \frac{5}{8} \times 24$$
$$= 15 \text{ cm}$$

Answer ..... cm [2]

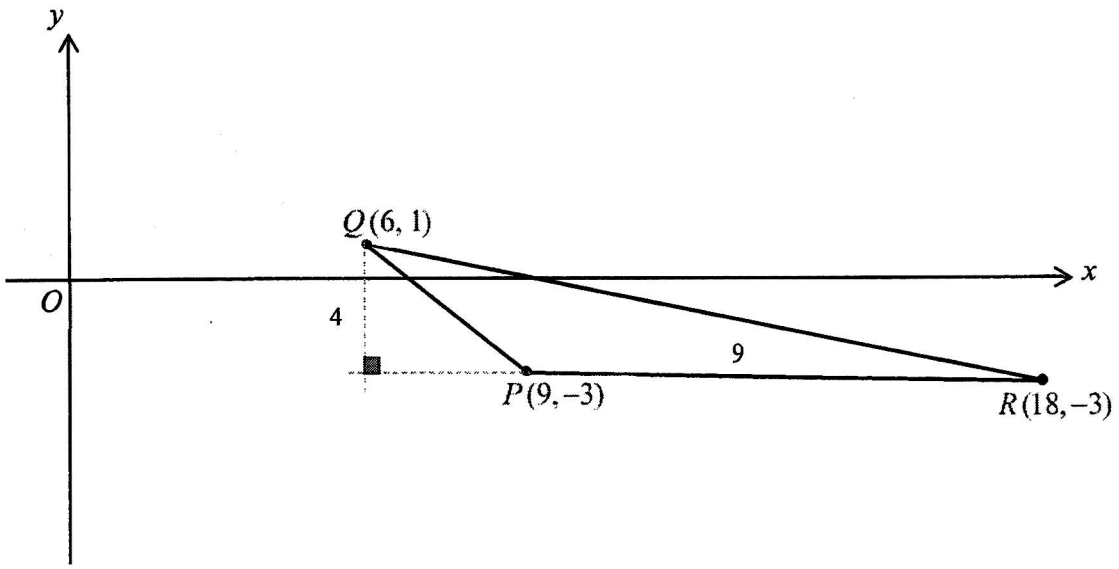
(b) The capacity of the smaller container is 0.45 litres.
Find the capacity of the larger container, giving your answer to 2 decimal places.

$$\text{Capacity of the larger container} = \left(\frac{8}{5}\right)^3 \times 0.45 \text{ litres}$$
$$= 1.8432 \text{ litres}$$
$$= 1.84 \text{ litres (2 decimal places)}$$

Answer ..... litres [1]

FREE TEST PAPERS - FREETESTPAPER.COM

22



In the diagram, the points P, Q and R have coordinates $(9,-3)$, $(6,1)$ and $(18,-3)$ respectively.

(a) Find the length of PQ.

$$PQ = \sqrt{(9-6)^2 + (-3-1)^2}$$
$$= \sqrt{3^2 + (-4)^2}$$
$$= 5 \text{ units}$$

Answer .....units [1]

(b) Find the value of $\cos \angle QPR$, giving your answer as a fraction in its simplest form.

$$\cos \angle QPR = -\frac{3}{5}$$

Some could not identify the right - angled triangle and some forget that $\cos A = -\cos\left(180^0 - A\right)$

Answer ..... [1]

(c) Find the area of triangle PQR.

$$\text{Area of triangle } PQR = \frac{1}{2} \times 9 \times 4 \text{ units}^2$$
$$= 18 \text{ units}^2$$

Some are using other more time-consuming methods such as "shoelace", $\frac{1}{2}ab\sin C$ even though the question is only 1 mark.

Answer ..... [1]

FREE TEST PAPERS - FREETESTPAPER.COM

(d) Find the equation of the line PQ.

$$\text{Gradient of } PQ = \frac{1-(-3)}{6-9}$$
$$= -\frac{4}{3}$$

$$\text{Equation of } PQ \text{ is } y-1=-\frac{4}{3}(x-6)$$
$$y-1=-\frac{4}{3}x+8$$
$$y=-\frac{4}{3}x+9 \quad \text{or } 4x+3y=27$$

Answer ..... [2]

(e) The equation of the line passing through the point R is $4x+21y=9$.

Find the coordinates of the point of intersection of this line and the line PQ.

$4x+3y=27$ ..... (1)
$4x+21y=9$ ..... (2)
(2) − (1):
$18y=-18$
$y=-1$
Sub $y=-1$ into (1):
$4x+3(-1)=27$
$4x=30$
$x=7\frac{1}{2}$

$\therefore$ The point of intersection is $\left(7\frac{1}{2}, -1\right)$.

Students must remember to put the brackets for the coordinates on their answer blank.

Answer ..... [3]

~ End of Paper ~

FREE TEST PAPERS - FREETESTPAPER.COM

BLANK PAGE

FREE TEST PAPERS - FREETESTPAPER.COM

Name:	Class:	Class Register Number:

中正中学

CHUNG CHENG HIGH SCHOOL (MAIN)

Chung Cheng High School Chung Cheng High School Chung Cheng High School Chung Cheng High School Chung Cheng High School
Chung Cheng High School Chung Cheng High School Chung Cheng High School Chung Cheng High School Chung Cheng High School
Chung Cheng High School Chung Cheng High School Chung Cheng High School Chung Cheng High School Chung Cheng High School
Chung Cheng High School Chung Cheng High School Chung Cheng High School Chung Cheng High School Chung Cheng High School
Chung Cheng High School Chung Cheng High School Chung Cheng High School Chung Cheng High School Chung Cheng High School

PRELIMINARY EXAMINATION 2021

SECONDARY 4

MATHEMATICS 4048/02

Paper 2 **Wednesday 1 September 2021**

2 hours 30 minutes

Candidates answer on the Question Paper

READ THESE INSTRUCTIONS FIRST

Write your name, class and index number in the spaces at the top of this page.
Write in dark blue or black pen.
You may use an HB pencil for any diagrams or graphs.
Do not use paper clips, glue or correction fluid.

Answer **all** questions.
If working is needed for any question it must be shown with the answer. Omission of essential working will result in loss of marks.
The use of an approved scientific calculator is expected, where appropriate. If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.
For π, use either your calculator value or 3.142, unless the question requires the answer in terms of π.

At the end of the examination, fasten all your work securely together.
The number of marks is given in brackets [ ] at the end of each question or part question.

The total number of marks for this paper is 100.

For Examiner's Use	
Question Number	Marks Obtained
1	
2	
3	
4	
5	
6	
7	
8	
9	
10	
Total Marks	

This document consists of **21** printed pages and **1** blank page.

[Turn Over

FREE TEST PAPERS - FREETESTPAPER.COM

Mathematical Formulae

Compound interest

$$\text{Total amount} = P\left(1+\frac{r}{100}\right)^n$$

Mensuration

$$\text{Curved surface area of a cone} = \pi r l$$

$$\text{Surface area of a sphere} = 4\pi r^2$$

$$\text{Volume of a cone} = \frac{1}{3}\pi r^2 h$$

$$\text{Volume of a sphere} = \frac{4}{3}\pi r^3$$

$$\text{Area of triangle } ABC = \frac{1}{2}ab\sin C$$

$$\text{Arc length} = r\theta \text{, where } \theta \text{ is in radians}$$

$$\text{Sector area} = \frac{1}{2}r^2\theta \text{, where } \theta \text{ is in radians}$$

Trigonometry

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc\cos A$$

Statistics

$$\text{Mean} = \frac{\Sigma fx}{\Sigma f}$$

$$\text{Standard deviation} = \sqrt{\frac{\Sigma fx^2}{\Sigma f} - \left(\frac{\Sigma fx}{\Sigma f}\right)^2}$$

FREE TEST PAPERS - FREETESTPAPER.COM

1 **(a)** Simplify $\left(\frac{a^6b^3}{8}\right)^{\frac{1}{3}} \div \frac{3b^{-1}}{a^2}$.

Answer ..... [3]

(b) Solve $\frac{2}{x-2}+\frac{3}{x+2}=0$.

Answer $x =$ ..... [2]

(c) Make q the subject in the equation $pq+9=p^2+3q$ and simplify your answer.

Answer ..... [3]

FREE TEST PAPERS - FREETESTPAPER.COM

(d) **(i)** Simplify $(4x+3y)^2+(3x-4y)^2$.

Answer ..... [2]

(ii) It is given that $x^2+y^2=1$. Using your answer in part **(i)**, explain why the maximum value of $(4x+3y)^2$ is 25.

Answer

[3]

FREE TEST PAPERS - FREETESTPAPER.COM

2 During nuclear fusion, it is observed that when two hydrogen atoms are fused together to form one helium atom, there is a loss in mass, M.

The atomic masses of one hydrogen atom and one helium atom are given in the table below. The masses are given in atomic mass unit (u).

Atom	Hydrogen	Helium
Atomic Mass (u)	2.0141	4.0026

(a) Find M (in u), leaving your answer in standard form.

Answer ..... u [2]

(b) Express M as a percentage of the atomic mass of one helium atom.

Answer ..... % [2]

(c) Given that $1\text{ u} = 1.66\times10^{-27}$ kg, find M in kilograms.

Answer ..... kg [1]

FREE TEST PAPERS - FREETESTPAPER.COM

3 Town P and Town Q are 40 km apart. A car is travelling from Town P to Town Q at an average speed of x km/h. During its return journey, the car later travelled back to Town P from Town Q at an average speed of $(x+8)$ km/h and the time taken for the return journey was 12 minutes less.

(i) Write down an equation to represent this information and show that it simplifies to $x^2+8x-1600=0$.

Answer

[4]

(ii) Solve the equation $x^2+8x-1600=0$, giving your solutions correct to two decimal places.

Answer $x =$ ..... or ..... [3]

FREE TEST PAPERS - FREETESTPAPER.COM

(iii) Given that the car left Town P at 09 00, find the time when the car reached Town Q. Give your answer correct to the nearest minute.

Answer ..... [2]

FREE TEST PAPERS - FREETESTPAPER.COM

4 The variables x and y are connected by the equation $y=\frac{3}{2}x+\frac{5}{x}-7$.

Some corresponding values of x and y are given in the table below.

x	0.5	1	1.5	2	3	4	5	6	7
y	3.75	–0.5	–1.42	p	–0.83	0.25	1.5	2.83	4.21

(a) Find the value of p. [1]

Answer $p=$ .....

(b) On the grid opposite, draw the graph of $y=\frac{3}{2}x+\frac{5}{x}-7$ for $0.5\le x\le 7$.

Use the scale of 2 cm to represent 1 unit on both axes. [3]

(c) By drawing a tangent, find the gradient of the curve at $x=2.5$.

Answer ..... [2]

(d) **(i)** On the grid in part **(b)**, draw the line $2y+x=2$ for $0\le x\le 7$.

[2]

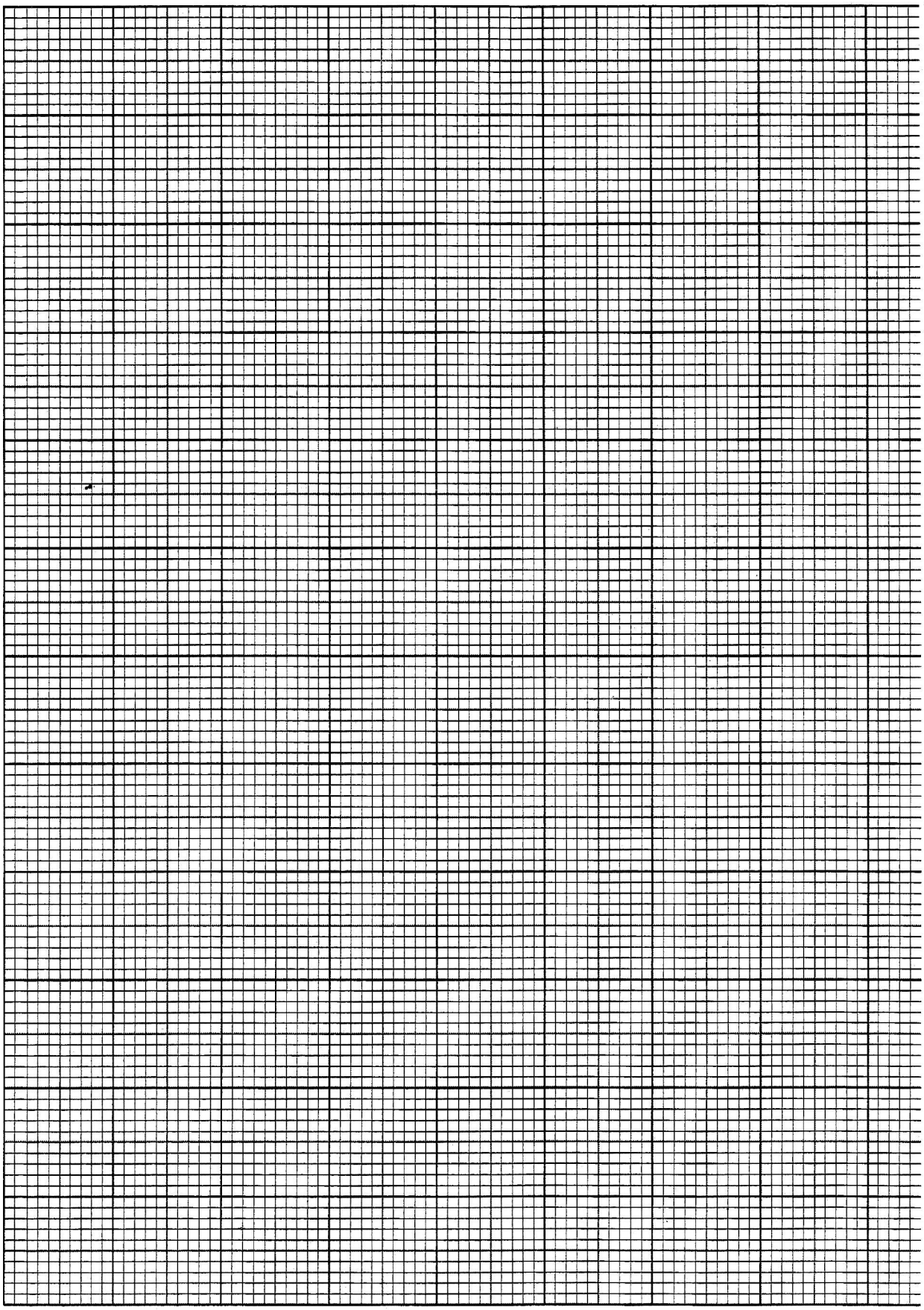
(ii) Write down the x-coordinates of the points where the line intersects the curve.

Answer $x=$ ..... or ..... [2]

(iii) Show that the points of intersection of the line and the curve give the solutions to the equation $2x^2-8x+5=0$.

[2]

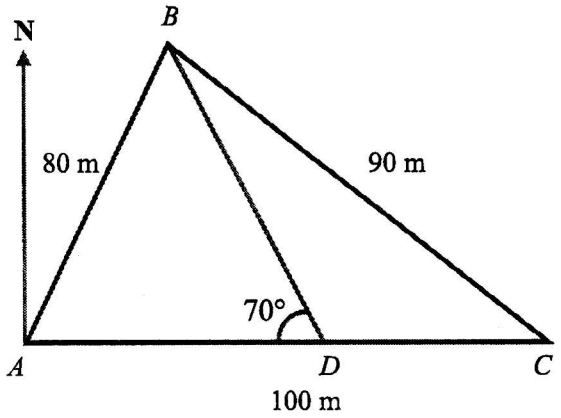
FREE TEST PAPERS - FREETESTPAPER.COM



FREE TEST PAPERS - FREETESTPAPER.COM

5 The diagram below shows three points, A, B and C on flat ground.

$AB = 80$ m, $AC = 100$ m and $BC = 90$ m. C is due east of A.



(a) (i) Show that angle $ACB = 49.5°$, correct to one decimal place.

[3]

(ii) Hence, calculate the bearing of C from B.

Answer ..... ° [2]

(iii) Point D lies along AC such that angle $BDA = 70°$. Find the distance CD.

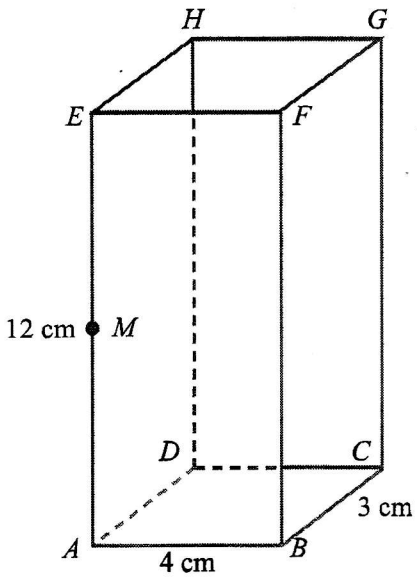
Answer ..... m [3]

FREE TEST PAPERS - FREETESTPAPER.COM

(iv) Find the ratio of area of triangle ABD to area of triangle BDC.
Give your answer correct to one decimal place.

Answer ..... [2]

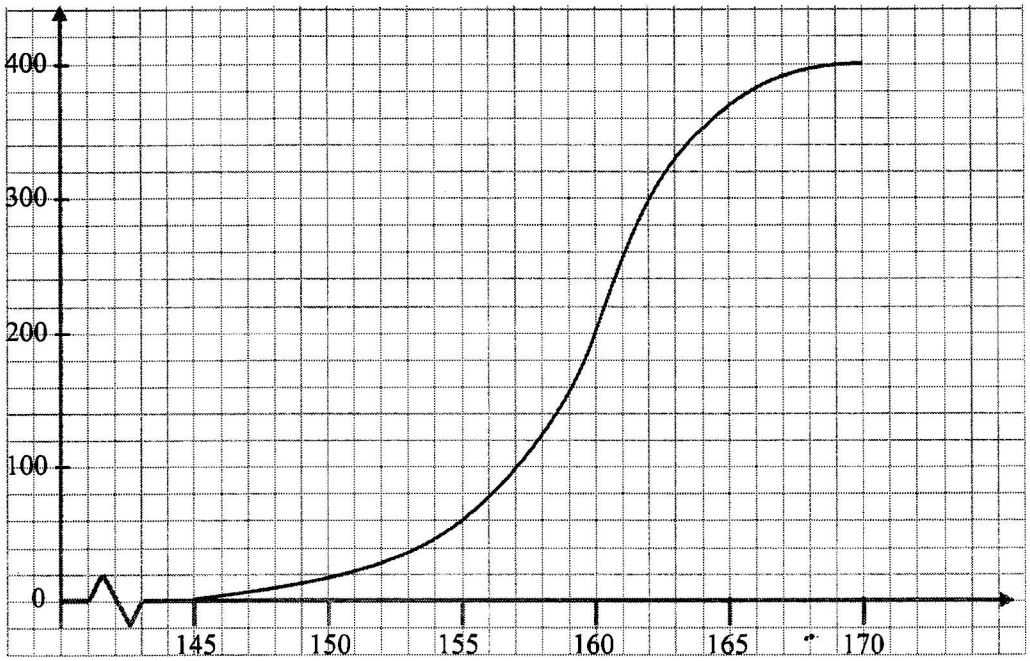
(b) The diagram below shows a cuboid with rectangular base $ABCD$.
$AB = 4$ cm, $BC = 3$ cm and $AE = 12$ cm. M is the midpoint of AE.
Find the angle of elevation of G from M.



Answer ..... [3]

FREE TEST PAPERS - FREETESTPAPER.COM

6 (a) The heights of 400 students in School *A* are recorded. The cumulative frequency curve below shows the distribution of their heights.



(i) State the median.

Answer ..... cm [1]

(ii) Find the interquartile range of the distribution.

Answer ..... cm [2]

(iii) In School *B*, the median and interquartile range of the heights of another 400 students are 165 cm and 8 cm respectively. Make two comments comparing the heights of students in School *A* and School *B*.

Answer

.....

.....

.....

.....

..... [2]

FREE TEST PAPERS - FREETESTPAPER.COM

(b) John flipped a coin five times and obtained five successive heads. Is it conclusive that the coin is biased? Explain your answer clearly.

Answer

.....

.....

.....

..... [2]

(c) A two-digit number is formed by drawing a random card from Bag *A* followed by another random card from Bag *B*. Bag *A* contains three cards labelled '1', '2' and '3'. Bag *B* contains three cards labelled '4', '5' and '7'. For example, drawing a '1' and "5" from Bag *A* and Bag *B* respectively will form the number '15'.

(i) Complete the possibility diagram below.

Bag *B* \ Bag *A*	1	2	3
4	**14**		
5		**25**	
7			

[2]

Find, as a fraction in its simplest form, the probability that the two-digit number formed is

(ii) odd,

Answer ..... [1]

(iii) a perfect square,

Answer ..... [1]

(iv) a prime number,

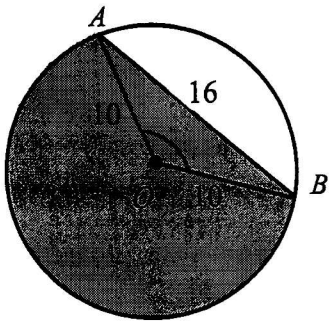
Answer ..... [1]

(v) a factor of 135.

Answer ..... [2]

FREE TEST PAPERS - FREETESTPAPER.COM

7 The diagram shows a circle, centre O, radius 10 cm. AB is a chord of length 16 cm.



(a) Show that angle $AOB = 1.855$ radians, correct to four significant figures.

Answer

[2]

Hence, find the

(b) perimeter of the shaded segment,

Answer ..... cm [3]

FREE TEST PAPERS - FREETESTPAPER.COM

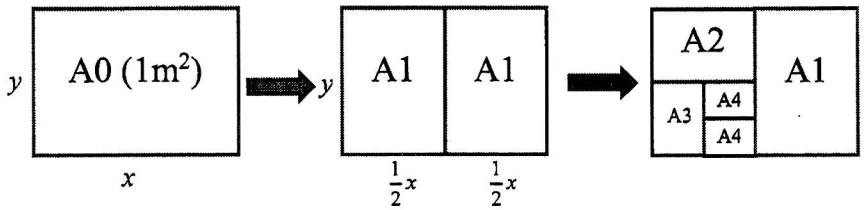
(c) area of the shaded segment.

Answer ..... cm^2 [2]

FREE TEST PAPERS - FREETESTPAPER.COM

8 A piece of A0-sized paper has a total surface area of 1 m^2. The length and breadth of the A0-sized paper are x m and y m respectively.

An A1 paper is an A0 paper folded in half, length-wise. An A2 paper is an A1 paper folded in half, so on and so forth.



(i) Write down the relationship between x and y.

Answer ..... [1]

(ii) Given that all A-sized papers are geometrically similar, show that $\frac{x}{y} = \sqrt{2}$.

Answer

[2]

(iii) Hence, using parts **(i)** and **(ii)**, find the values of x and y.

Answer x =....., y = ... [4]

FREE TEST PAPERS - FREETESTPAPER.COM

(iv) Write down the dimensions of an A4-sized paper in millimetres.

Answer ..... mm × ..... mm [2]

(v) Given that N is an integer, express the number of pieces of AN-sized paper that can be cut out from an A0-sized paper in terms of N.

Answer ..... [1]

FREE TEST PAPERS - FREETESTPAPER.COM

9 Robert has 3 options to get to school every weekday morning.

Option **A**: He takes the bus.

Option **B**: He takes the MRT.

Option **C**: He takes a taxi.

The matrices **A**, **B** and **C** represent his journey to school if he were to choose option **A**, **B** or **C** respectively.

$$\mathbf{A}=\begin{array}{c}\begin{matrix}\text{Bus} & \text{MRT} & \text{Taxi}\end{matrix}\\\begin{pmatrix}1 & 0 & 0\\0 & 0 & 0\\0 & 0 & 0\end{pmatrix}\end{array},\quad \mathbf{B}=\begin{array}{c}\begin{matrix}\text{Bus} & \text{MRT} & \text{Taxi}\end{matrix}\\\begin{pmatrix}0 & 0 & 0\\0 & 1 & 0\\0 & 0 & 0\end{pmatrix}\end{array},\quad \mathbf{C}=\begin{array}{c}\begin{matrix}\text{Bus} & \text{MRT} & \text{Taxi}\end{matrix}\\\begin{pmatrix}0 & 0 & 0\\0 & 0 & 0\\0 & 0 & 1\end{pmatrix}\end{array}.$$

(a) In a particular week, Robert took the bus 3 times. He took the MRT and taxi in each of the other two days. The above information can be represented by a matrix **S** where $\mathbf{S}=3\mathbf{A}+\mathbf{B}+\mathbf{C}$. Find **S**.

Answer ..... [2]

(b) The table below shows the travelling time taken, in minutes, for each of the 3 options that Robert can take to get to school.

Option	Bus	MRT	Taxi
Time taken (in minutes)	30	20	15

(i) Write down a column matrix **N** to represent the information in the table.

Answer **N** = ... [1]

FREE TEST PAPERS - FREETESTPAPER.COM

(ii) Evaluate the matrix **SN**.

Answer **SN** = ... [2]

(iii) State what the elements in matrix **SN** represent.

Answer

.....

.....

.....

..... [1]

(c) Write down a matrix **J** such that product of **J** and the answer in part **(b)(ii)** will give the average travelling time taken by Robert in a particular week.

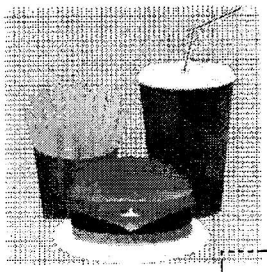
Answer ..... [1]

(d) Hence, find the average travelling time taken by Robert per day in a particular week.

Answer ..... minutes [2]

FREE TEST PAPERS - FREETESTPAPER.COM

10 The diagram below shows the menu from a fast food restaurant.



Combo A
- Burger
- Medium Fries
- Medium Drink

$5.90 only!

Upsize *your drink and fries to Large-size for only* $1.10

Ala carte	Medium ($)	Large ($)
Burger (1 size)	3.20	
Fries	2.20	2.90
Drink	2.80	3.60

(a) Albert wants to buy a burger for both himself and his brother Bart. His brother wants at least a medium-sized fries. Albert wants a large drink while Bart wants a medium drink.

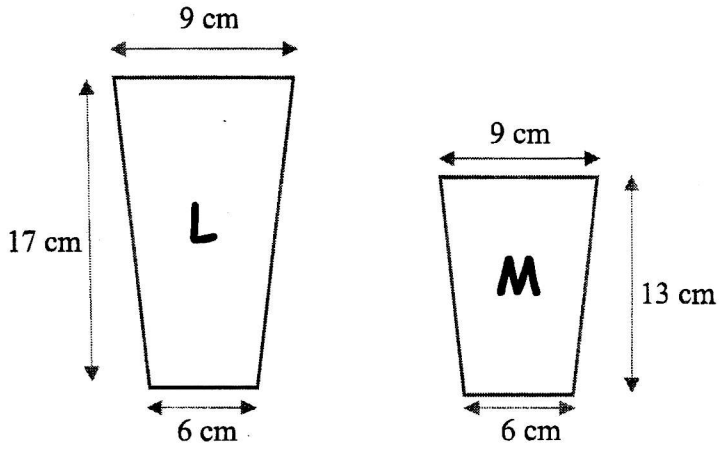
By considering three options, suggest how Albert should place his order.
Justify any decisions that you make and show your calculations clearly.

Answer

[4]

FREE TEST PAPERS - FREETESTPAPER.COM

(b) The diagram below shows the cross-sectional area of the large (L) and medium (M) drink cups sold by the fast food restaurant in part **(a)**. The Large and Medium cups have a height of 17 cm and 13 cm respectively. The top and bottom **diameters** of both cups are 9 cm and 6 cm respectively



The volume of a cup is given by $V = \frac{1}{3}\pi h\left(R^2 + Rr + r^2\right)$ where h is the height, R and r are the radii of the top and bottom of the cup respectively. Using the information from part **(a)**, determine whether the medium cup or large cup gives better value for money.

Answer

[4]

FREE TEST PAPERS - FREETESTPAPER.COM

BLANK PAGE

FREE TEST PAPERS - FREETESTPAPER.COM

ANS

Name:	Class:	Class Register Number:

中正中学

CHUNG CHENG HIGH SCHOOL (MAIN)

Chung Cheng High School Chung Cheng High School Chung Cheng High School Chung Cheng High School Chung Cheng High School
Chung Cheng High School Chung Cheng High School Chung Cheng High School Chung Cheng High School Chung Cheng High School
Chung Cheng High School Chung Cheng High School Chung Cheng High School Chung Cheng High School Chung Cheng High School
Chung Cheng High School Chung Cheng High School Chung Cheng High School Chung Cheng High School Chung Cheng High School
Chung Cheng High School Chung Cheng High School Chung Cheng High School Chung Cheng High School Chung Cheng High School

PRELIMINARY EXAMINATION 2021

SECONDARY 4

MATHEMATICS 4048/02

Paper 2 **Wednesday 1 September 2021**

2 hours 30 minutes

Candidates answer on the Question Paper

READ THESE INSTRUCTIONS FIRST

Write your name, class and index number in the spaces at the top of this page.
Write in dark blue or black pen.
You may use an HB pencil for any diagrams or graphs.
Do not use paper clips, glue or correction fluid.

Answer **all** questions.
If working is needed for any question it must be shown with the answer. Omission of essential working will result in loss of marks.
The use of an approved scientific calculator is expected, where appropriate. If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.
For π, use either your calculator value or 3.142, unless the question requires the answer in terms of π.

At the end of the examination, fasten all your work securely together.
The number of marks is given in brackets [ ] at the end of each question or part question.

The total number of marks for this paper is 100.

For Examiner's Use	
Question Number	Marks Obtained
1	
2	
3	
4	
5	
6	
7	
8	
9	
10	
Total Marks	

This document consists of **21** printed pages and **1** blank page.

[Turn Over

FREE TEST PAPERS - FREETESTPAPER.COM

Mathematical Formulae

Compound interest

$$\text{Total amount} = P\left(1+\frac{r}{100}\right)^n$$

Mensuration

$$\text{Curved surface area of a cone} = \pi r l$$

$$\text{Surface area of a sphere} = 4\pi r^2$$

$$\text{Volume of a cone} = \frac{1}{3}\pi r^2 h$$

$$\text{Volume of a sphere} = \frac{4}{3}\pi r^3$$

$$\text{Area of triangle } ABC = \frac{1}{2}ab\sin C$$

$$\text{Arc length} = r\theta \text{, where } \theta \text{ is in radians}$$

$$\text{Sector area} = \frac{1}{2}r^2\theta \text{, where } \theta \text{ is in radians}$$

Trigonometry

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc\cos A$$

Statistics

$$\text{Mean} = \frac{\Sigma fx}{\Sigma f}$$

$$\text{Standard deviation} = \sqrt{\frac{\Sigma fx^2}{\Sigma f} - \left(\frac{\Sigma fx}{\Sigma f}\right)^2}$$

FREE TEST PAPERS - FREETESTPAPER.COM

1 **(a)** Simplify $\left(\frac{a^6b^3}{8}\right)^{\frac{1}{3}} \div \frac{3b^{-1}}{a^2}$.

$$\left(\frac{a^6b^3}{8}\right)^{\frac{1}{3}} \div \frac{3b^{-1}}{a^2} = \frac{a^2b}{2} \times \frac{a^2}{3b^{-1}}$$

$$= \frac{a^2b}{2} \times \frac{a^2b}{3} \quad [\text{M2} - \text{Any 2 Laws of Indices}]$$

$$= \frac{a^4b^2}{6} \quad [\text{A1}]$$

Answer ..... [3]

(b) Solve $\frac{2}{x-2} + \frac{3}{x+2} = 0$.

$$\frac{2(x+2)+3(x-2)}{(x-2)(x+2)} = 0 \quad [\text{M1} - \text{Single Fraction}]$$

$$2x+4+3x-6=0$$

$$5x-2=0$$

$$x = \frac{2}{5} \text{ or } 0.4 \quad [\text{A1}]$$

Answer $x =$ ..... [2]

(c) Make q the subject in the equation $pq+9 = p^2+3q$ and simplify your answer.

$$pq+9 = p^2+3q$$

$$pq-3q = p^2-9 \quad [\text{M1} - \text{Grouping } q \text{ terms}]$$

$$q(p-3) = (p-3)(p+3) \quad [\text{M1} - \text{Difference of squares}]$$

$$q = \frac{(p-3)(p+3)}{p-3}$$

$$q = p+3 \quad [\text{A1}]$$

Answer ..... [3]

FREE TEST PAPERS - FREETESTPAPER.COM

(d) **(i)** Simplify $(4x+3y)^2+(3x-4y)^2$.

$(4x+3y)^2+(3x-4y)^2$

$=16x^2+24xy+9y^2+9x^2-24xy+16y^2$ [M1 – Expansion]

$=25x^2+25y^2$

$=25(x^2+y^2)$ } [A1]

Answer ..... [2]

(ii) It is given that $x^2+y^2=1$. Using your answer in part **(i)**, explain why the maximum value of $(4x+3y)^2$ is 25.

$(4x+3y)^2+(3x-4y)^2=25(x^2+y^2)$

$=25(1)$ [$\sqrt{\text{M1}}$ – Substitute for $x^2+y^2=1$]

$=25$

$(4x+3y)^2=25-(3x-4y)^2$ [B1]

Since $(3x-4y)^2\geq 0$, $-(3x-4y)^2\leq 0$ [A1 – Recognising that $(3x-4y)^2\geq 0$]

$25-(3x-4y)^2\leq 25$

$(4x+3y)^2\leq 25$

Max value of $(4x+3y)^2=25$ (shown) [AG]

[3]

FREE TEST PAPERS - FREETESTPAPER.COM

2 During nuclear fusion, it is observed that when two hydrogen atoms are fused together to form one helium atom, there is a loss in mass, M.

The atomic masses of one hydrogen atom and one helium atom are given in the table below. The masses are given in atomic mass unit (u).

Atom	Hydrogen	Helium
Atomic Mass (u)	2.0141	4.0026

(a) Find M (in u), leaving your answer in standard form.

$M_D = \mathrm{H} + \mathrm{H} - \mathrm{He}$

$= 2.0141 + 2.0141 - 4.0026$ [B1 – Substituting correct values]

$= 0.0256$

$= 2.56 \times 10^{-2}$ [B1 – Correct Answer]

Answer ..... u [2]

(b) Express M as a percentage of the atomic mass of one helium atom.

$\frac{M}{\mathrm{He}} \times 100\% = \frac{2.56 \times 10^{-2}}{4.0026} \times 100\%$ [M1 – Subtitution of values]

$= 0.639585$

$= 0.640$ (3 sig. fig.) [A1]

Answer ..... % [2]

(c) Given that $1\,\mathrm{u} = 1.66 \times 10^{-27}$ kg, find M in kilograms.

mass $= (1.66 \times 10^{-27})M$

$= (1.66 \times 10^{-27})(0.0256)$

$= 0.042496 \times 10^{-27}$

$= 4.2496 \times 10^{-29}$

$= 4.25 \times 10^{-29}$ kg (3 sig. fig.) [B1 for either]

Answer ..... kg [1]

FREE TEST PAPERS - FREETESTPAPER.COM

3 Town P and Town Q are 40 km apart. A car is travelling from Town P to Town Q at an average speed of x km/h. During its return journey, the car later travelled back to Town P from Town Q at an average speed of $(x+8)$ km/h and the time taken for the return journey was 12 minutes less.

(i) Write down an equation to represent this information and show that it simplifies to $x^2+8x-1600=0$.

Answer

$\frac{40}{x}-\frac{40}{x+8}=\frac{1}{5}$ [M1 – Correct expression for time (either)]

[B1 – Forming equation with $\frac{1}{5}$]

$\frac{40(x+8)-40x}{x(x+8)}=\frac{1}{5}$ [M1 – Single fraction]

$\frac{320}{x^2+8x}=\frac{1}{5}$ [M1 – Simplifying]

$x^2+8x=1600$

$x^2+8x-1600=0$ (*shown*) [AG]

[4]

(ii) Solve the equation $x^2+8x-1600=0$, giving your solutions correct to two decimal places.

$x^2+8x-1600=0$

$x=\frac{-8\pm\sqrt{8^2-4(1)((-1600))}}{2(1)}$ [M1 – Formula or completing the square]

$=\frac{-8\pm\sqrt{6464}}{2}$

$x=36.199$ or $x=-44.199$

$x=36.20$ or $x=-44.20$ (2 dec. places) [A1 each]

Note: –1 mark if left in 3 sig. fig.

Answer $x=$ ..... or ..... [3]

FREE TEST PAPERS - FREETESTPAPER.COM

(iii) Given that the car left Town P at 0900, find the time when the car reached Town Q. Give your answer correct to the nearest minute.

Since $x > 0, x = 36.199$

$$\text{Time taken} = \frac{40}{36.199} \quad [\text{M1} - \text{Time formula}]$$

$$= 1.10498 \text{ hours}$$

Time $= 1006$ [A1]

Answer ..... [2]

FREE TEST PAPERS - FREETESTPAPER.COM

4 The variables x and y are connected by the equation $y=\frac{3}{2}x+\frac{5}{x}-7$.

Some corresponding values of x and y are given in the table below.

x	0.5	1	1.5	2	3	4	5	6	7
y	3.75	–0.5	–1.42	p	–0.83	0.25	1.5	2.83	4.21

(a) Find the value of p. [1]

–1.5 [B1]

Answer $p=$ .....

(b) On the grid opposite, draw the graph of $y=\frac{3}{2}x+\frac{5}{x}-7$ for $0.5\le x\le 7$.

Use the scale of 2 cm to represent 1 unit on both axes. [3]

(c) By drawing a tangent, find the gradient of the curve at $x=2.5$.

From graph,
Drawing tangent [M1]
Gradient = 0.7 [0.6 – 0.8] [A1]

Answer ..... [2]

(d) **(i)** On the grid in part **(b)**, draw the line $2y+x=2$ for $0\le x\le 7$.

$2y+x=2$
$2y=-x+2$ [M1 – Make y the subject]
$y=-\frac{1}{2}x+1$ [G1 – Draw y] [G2 – If draw graph only]

[2]

(ii) Write down the x-coordinates of the points where the line intersects the curve.

$x=0.75$ [0.7 – 0.8], $x=3.25$ [3.2 – 3.3] [A1]

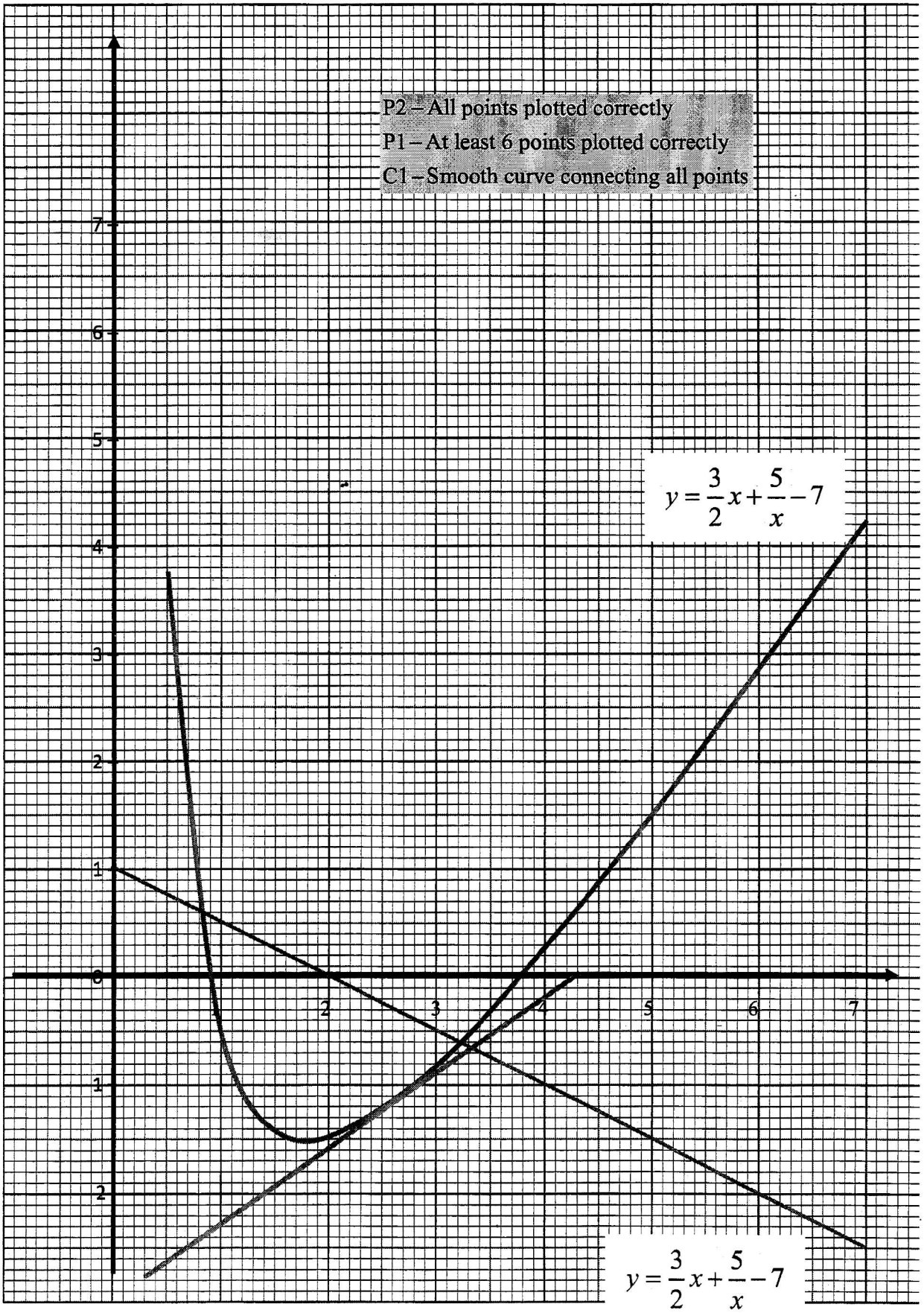
Answer $x=$ ..... or ..... [2]

(iii) Show that the points of intersection of the line and the curve give the solutions to the equation $2x^2-8x+5=0$.

$\frac{3}{2}x+\frac{5}{x}-7=-\frac{1}{2}x+1$ [M1 – Equating]
$3x^2+10-14x=-x^2+2x$
$4x^2-16x+10=0$ [A1]
$2x^2-8x+5=0$ [AG]

Answer ..... [2]

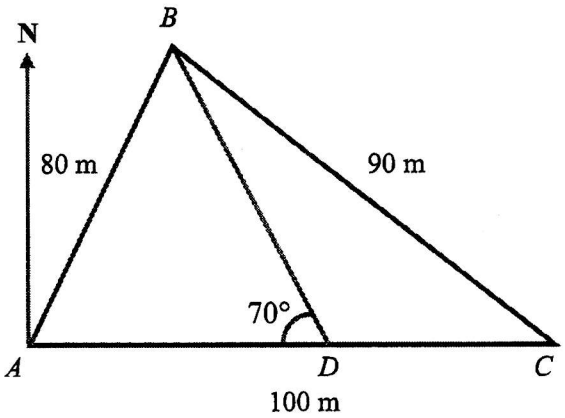
FREE TEST PAPERS - FREETESTPAPER.COM



FREE TEST PAPERS - FREETESTPAPER.COM

5 The diagram below shows three points, A, B and C on flat ground.

$AB = 80$ m, $AC = 100$ m and $BC = 90$ m. C is due east of A.



(a) (i) Show that angle $ACB = 49.5°$, correct to one decimal place.

$$\cos \angle ACB = \frac{90^2 + 100^2 - 80^2}{2(90)(100)} \quad [\text{M1} - \text{Cosine Rule or other method}]$$

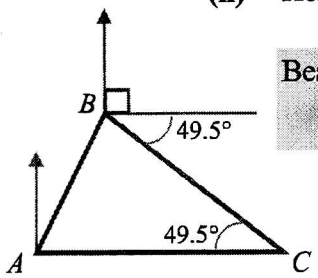
$$\angle ACB = \cos^{-1}\left(\frac{90^2 + 100^2 - 80^2}{2(90)(100)}\right) \quad [\text{M1} - \text{Cos } C \text{ the subject}]$$

$$= 49.458° \quad [\text{A1}]$$

$$= 49.5° \quad (\text{shown})$$

[3]

(ii) Hence, calculate the bearing of C from B.



Bearing of C from $B = 90° + 49.458°$ [M1 – 90° due east]

$= 139.5°$ (1 dec. place) [A1]

Answer ..... ° [2]

(iii) Point D lies along AC such that angle $BDA = 70°$. Find the distance CD.

$\angle BDC = 180° - 70°$ (Adjacent $\angle$s on a straight line)

$= 110°$

$\angle CBD = 180° - 110° - 49.458°$

$= 20.542°$ [M1 – Finding $\angle CBD$]

$$\frac{90}{\sin 110°} = \frac{CD}{\sin 20.542°} \quad [\text{M1} - \text{Sine Rule}]$$

$$CD = \frac{90 \sin 20.542°}{\sin 110°}$$

$= 33.606$

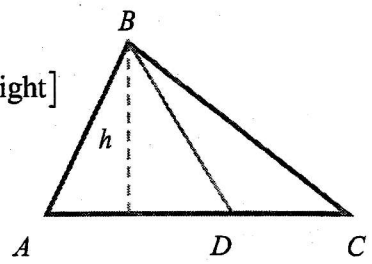
$= 33.6$ m (3 sig. fig.) [A1]

Answer ..... m [3]

FREE TEST PAPERS - FREETESTPAPER.COM

(iv) Find the ratio of area of triangle ABD to area of triangle BDC.
Give your answer correct to one decimal place.

Since they share a common height,



$$\frac{\text{Area of } \Delta ABD}{\text{Area of } \Delta BDC} = \frac{\frac{1}{2}(AD)(h)}{\frac{1}{2}(DC)(h)} \quad [\text{M1} - \text{Compare ratio with common height}]$$

$$= \frac{AD}{CD}$$

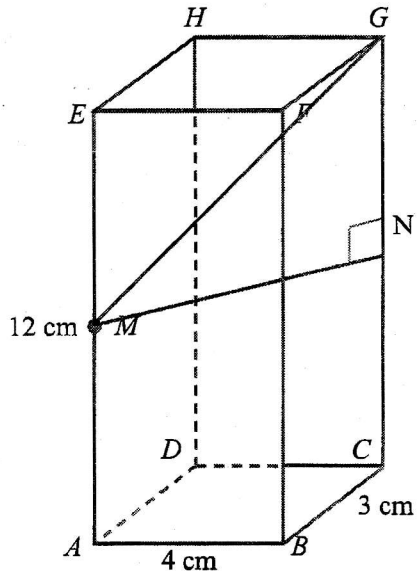
$$= \frac{100 - 33.606}{33.606}$$

$$= 1.975$$

$$= 2.0 \text{ (1 dec. place)} \quad [\text{A1} - \text{Accept } 2.0:1.0]$$

Answer ..... [2]

(b) The diagram below shows a cuboid with rectangular base $ABCD$.
$AB = 4$ cm, $BC = 3$ cm and $AE = 12$ cm. M is the midpoint of AE.
Find the angle of elevation of G from M.



Let N be midpoint of GC.

$$AC = \sqrt{4^2 + 3^2}$$

$$= 5 \text{ cm} \quad [\text{M1} - \text{Finding } AC]$$

$$GN = \frac{12}{2} = 6 \text{ cm}$$

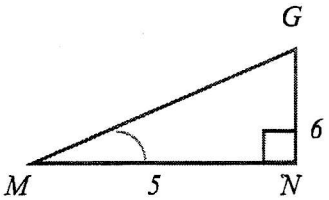
$$\tan \angle GMN = \frac{GN}{MN}$$

$$= \frac{6}{5} \quad [\text{M1} - \text{Using tangent}]$$

$$\angle GMN = \tan^{-1}\left(\frac{6}{5}\right)$$

$$= 50.194°$$

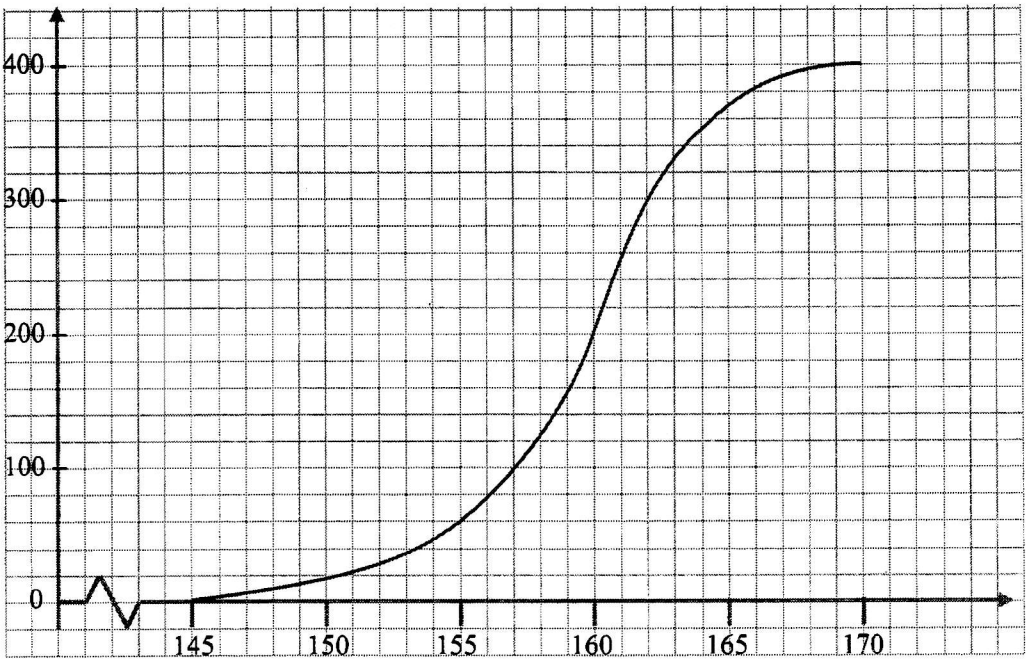
$$= 50.2° \text{ (1 dec. place)} \quad [\text{A1}]$$



Answer ..... [3]

FREE TEST PAPERS - FREETESTPAPER.COM

6 (a) The heights of 400 students in School *A* are recorded. The cumulative frequency curve below shows the distribution of their heights.



(i) State the median.

160 cm [B1]

Answer ..... cm [1]

(ii) Find the interquartile range of the distribution.

$Q_1 = 157$, $Q_3 = 162$
IQR $= 162 - 157$ [B1]
$= 5$ cm [B1]

Answer ..... cm [2]

(iii) In School *B*, the median and interquartile range of the heights of another 400 students are 165 cm and 8 cm respectively. Make two comments comparing the heights of students in School *A* and School *B*.

Answer

The students in School *B* are generally taller as they have a higher median of .....

165 cm as compared to School *A* (160 cm). .....

.....

The height of students in School *B* are generally more widespread as they have a .....

higher interquartile range of 8 cm as compared to School *A* (5 cm). [B1 each] .....

[2]

FREE TEST PAPERS - FREETESTPAPER.COM

(b) John flipped a coin five times and obtained five successive heads. Is it conclusive that the coin is biased? Explain your answer clearly.

Answer

No, given that John only flipped the coin 5 times, there is a 1 in 32 chance that of obtaining 5 successive heads which is still possible. The sample size is **too small** for any logical conclusion that the coin is biased.

..... [2]

(c) A two-digit number is formed by drawing a random card from Bag *A* followed by another random card from Bag *B*. Bag *A* contains three cards labelled '1', '2' and '3'. Bag *B* contains three cards labelled '4', '5' and '7'. For example, drawing a '1' and "5" from Bag *A* and Bag *B* respectively will form the number '15'.

(i) Complete the possibility diagram below.

Any 1 row correct [B1]
All rows correct [B2]

Bag *B* \ Bag *A*	1	2	3
4	**14**	24	34
5	15	**25**	35
7	17	27	37

[2]

Find, as a fraction in its simplest form, the probability that the two-digit number formed is

(ii) odd,

$\frac{2}{3}$ [B1]

Answer ..... [1]

(iii) a perfect square,

$P(\text{Number is a perfect square}) = P(\text{Number is } 25)$
$= \frac{1}{9}$ [B1]

..... [1]

(iv) a prime number,

$P(\text{Number is prime}) = P(\text{Number is } 17, 37)$
$= \frac{2}{9}$ [B1]

..... [1]

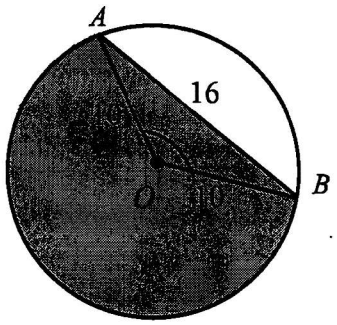
(v) a factor of 135.

$135 = 3 \times 3 \times 3 \times 5$ [M1 – Prime factorisation of 135]
Factors of 135 are : 1, 3, 5, 9, 15, 27, 45, 135
$P(\text{Factor of } 135) = P(15, 27)$
$= \frac{2}{9}$ [A1]

Answer ..... [2]

FREE TEST PAPERS - FREETESTPAPER.COM

7 The diagram shows a circle, centre O, radius 10 cm. AB is a chord of length 16 cm.



(a) Show that angle $AOB = 1.855$ radians, correct to four significant figures.

Answer

$$\sin\frac{\angle AOB}{2} = \frac{8}{10}$$

$$\angle AOB = 2\sin^{-1}\frac{8}{10} \qquad [\text{M1} - \text{Any method}]$$

$$= 1.8545 \qquad [\text{A1}]$$

$$= 1.855 \text{ rad (shown)} \quad [\text{AG}]$$

[2]

Hence, find the

(b) perimeter of the shaded segment,

$$\text{Perimeter} = (2\pi - 1.8545)(10) + 16 \quad [\text{M1, M1}]$$

$$= 60.28$$

$$= 60.3 \text{ cm (3 sig. fig.)} \quad [\text{A1}]$$

Answer ..... cm [3]

FREE TEST PAPERS - FREETESTPAPER.COM

(c) area of the shaded segment.

Area of shaded segment $= \frac{1}{2}(10)^2(2\pi - 1.8545) + \frac{1}{2}(10)^2 \sin 1.8545$

[M1 – Area of sector or Area of triangle]

$= 269.43$

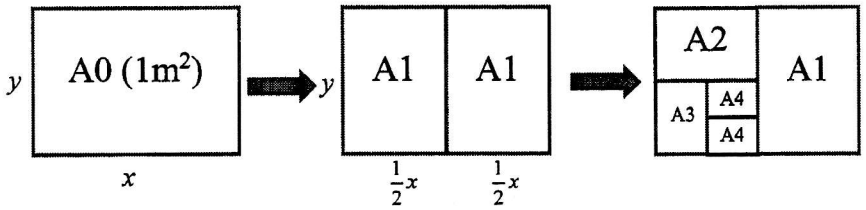
$= 269 \text{ cm}^2$ (3 sig. fig.) [A1]

Answer ..... cm^2 [2]

FREE TEST PAPERS - FREETESTPAPER.COM

8 A piece of A0-sized paper has a total surface area of 1 m^2. The length and breadth of the A0-sized paper are x m and y m respectively.

An A1 paper is an A0 paper folded in half, length-wise. An A2 paper is an A1 paper folded in half, so on and so forth.



(i) Write down the relationship between x and y.

$xy = 1$ [B1 oe]

Answer ..... [1]

(ii) Given that all A-sized papers are geometrically similar, show that $\frac{x}{y} = \sqrt{2}$.

Since the papers are geometrically similar, ratio of corresponding sides are equal.

$$\frac{length_{A0}}{breadth_{A0}} = \frac{length_{A1}}{breadth_{A1}}$$

$$\frac{x}{y} = \frac{y}{\left(\frac{1}{2}x\right)} \quad [\text{M1 or similar}]$$

$$\frac{x^2}{y^2} = 2 \quad [\text{A1}]$$

$$\frac{x}{y} = \sqrt{2} \ (\text{Shown}) \quad [\text{AG}]$$

[2]

(iii) Hence, using parts **(i)** and **(ii)**, find the values of x and y.

$xy = 1$

$y = \frac{1}{x} \quad ---(1)$ [M1 – Making x or y the subject]

$\frac{x}{y} = \sqrt{2} \quad ---(2)$

Substitute (1) into (2):

$$\frac{x}{y} = \sqrt{2}$$

$$\frac{x}{\left(\frac{1}{x}\right)} = \sqrt{2} \quad [\text{M1 – Substitution}]$$

$$x^2 = \sqrt{2}$$

$$x = \sqrt{\sqrt{2}} \quad [\text{M1 – Solving}]$$

$$= 1.1892..$$

$$= 1.19$$

$y = 0.841$ (3 sig. fig) [A1 – Both answers correct]

[4]

FREE TEST PAPERS - FREETESTPAPER.COM

(iv) Write down the dimensions of an A4-sized paper in millimetres.

$$x = \frac{1.1892 \times 1000}{4}$$
$$= 297 \ (3 \ sig \ fig) \ [\text{M1} - \text{Converting to mm}]$$

$$y = \frac{0.84089 \times 1000}{4}$$
$$= 210 \ (3 \ sig \ fig)) [\text{A1} - \text{Both correct}] [\text{B2} - \text{Both correct}]$$

Answer ..... mm × ..... mm [2]

(v) Given that N is an integer, express the number of pieces of AN-sized paper that can be cut out from an A0-sized paper in terms of N.

Number of pieces $= 2^N$ [B1]

Answer ..... [1]

FREE TEST PAPERS - FREETESTPAPER.COM

9 Robert has 3 options to get to school every weekday morning.

Option **A**: He takes the bus.

Option **B**: He takes the MRT.

Option **C**: He takes a taxi.

The matrices **A**, **B** and **C** represent his journey to school if he were to choose option **A**, **B** or **C** respectively.

$$\mathbf{A}=\begin{array}{c}\begin{matrix}\text{Bus} & \text{MRT} & \text{Taxi}\end{matrix}\\ \begin{pmatrix}1 & 0 & 0\\ 0 & 0 & 0\\ 0 & 0 & 0\end{pmatrix}\end{array},\quad \mathbf{B}=\begin{array}{c}\begin{matrix}\text{Bus} & \text{MRT} & \text{Taxi}\end{matrix}\\ \begin{pmatrix}0 & 0 & 0\\ 0 & 1 & 0\\ 0 & 0 & 0\end{pmatrix}\end{array},\quad \mathbf{C}=\begin{array}{c}\begin{matrix}\text{Bus} & \text{MRT} & \text{Taxi}\end{matrix}\\ \begin{pmatrix}0 & 0 & 0\\ 0 & 0 & 0\\ 0 & 0 & 1\end{pmatrix}\end{array}.$$

(a) In a particular week, Robert took the bus 3 times. He took the MRT and taxi in each of the other two days. The above information can be represented by a matrix **S** where $\mathbf{S}=3\mathbf{A}+\mathbf{B}+\mathbf{C}$. Find **S**.

$$\mathbf{S}=3\begin{pmatrix}1 & 0 & 0\\ 0 & 0 & 0\\ 0 & 0 & 0\end{pmatrix}+\begin{pmatrix}0 & 0 & 0\\ 0 & 1 & 0\\ 0 & 0 & 0\end{pmatrix}+\begin{pmatrix}0 & 0 & 0\\ 0 & 0 & 0\\ 0 & 0 & 1\end{pmatrix} \quad [\text{M1}]$$

$$=\begin{pmatrix}3 & 0 & 0\\ 0 & 1 & 0\\ 0 & 0 & 1\end{pmatrix} \quad [\text{A1}]$$

Answer ..... [2]

(b) The table below shows the travelling time taken, in minutes, for each of the 3 options that Robert can take to get to school.

Option	Bus	MRT	Taxi
Time taken (in minutes)	30	20	15

(i) Write down a column matrix **N** to represent the information in the table.

$$\mathbf{N}=\begin{pmatrix}30\\ 20\\ 15\end{pmatrix} \quad [\text{B1}]$$

Answer $\mathbf{N}=$ ..... [1]

FREE TEST PAPERS - FREETESTPAPER.COM

(ii) Evaluate the matrix **SN**.

$$\mathbf{SN} = \begin{pmatrix} 3 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}\begin{pmatrix} 30 \\ 20 \\ 15 \end{pmatrix} = \begin{pmatrix} 3(30) \\ 1(20) \\ 1(15) \end{pmatrix} \quad [\text{M1}]$$

$$= \begin{pmatrix} 90 \\ 20 \\ 15 \end{pmatrix} \quad [\text{A1}]$$

Answer **SN** = ... [2]

(iii) State what the elements in matrix **SN** represent.

Answer

The elements represent the total time taken in minutes, in that particular week by Robert to go to school by via option *A*, *B* and *C* respectively. [1]

(c) Write down a matrix **J** such that product of **J** and the answer in part **(b)(ii)** will give the average travelling time taken by Robert in a particular week.

$\mathbf{J} = (0.2 \quad 0.2 \quad 0.2)$ [B1 – Accept fractions]

Answer ..... [1]

(d) Hence, find the average travelling time taken by Robert per day in a particular week.

$$\mathbf{J}(\mathbf{SN}) = (0.2 \quad 0.2 \quad 0.2)\begin{pmatrix} 90 \\ 20 \\ 15 \end{pmatrix} \quad [\text{M1} - \text{FT but order must be correct}]$$

$$= (18 + 4 + 3)$$

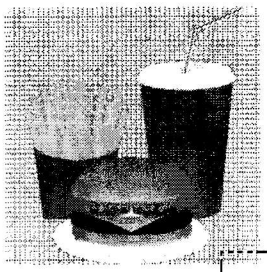
$$= (25) \quad [\text{B1} - \text{with brackets}]$$

Average time taken is 25 minutes

Answer ..... minutes [2]

FREE TEST PAPERS - FREETESTPAPER.COM

10 The diagram below shows the menu from a fast food restaurant.



Combo A
- Burger
- Medium Fries
- Medium Drink

$5.90 only!

***Upsize** your drink and fries to Large-size for only $1.10*

Ala carte	Medium ($)	Large ($)
Burger (1 size)	3.20	
Fries	2.20	2.90
Drink	2.80	3.60

(a) Albert wants to buy a burger for both himself and his brother Bart. His brother wants at least a medium-sized fries. Albert wants a large drink while Bart wants a medium drink.

By considering **three options**, suggest how Albert should place his order.

Justify any decisions that you make and show your calculations clearly.

Answer

Choose 3 out of the 4 possible options

Option A: (Combo A + Upsize) + (Burger + Medium Drink)

Total cost = $ 5.90 + 1.10 + 3.20 + 2.80

= $13.00 [B1]

Option B: Combo A + Combo A + Upsize

Total cost = $ 5.90 + 5.90 + 1.10

= $12.90 [B1]

Option C: 2 × Burger + M.Fries + M.Drink + L.Drink

Total cost = $2(3.20) + 2.20 + 2.80 + 3.60

= $15.00 [B1]

Option D: ComboA + Burger + L.Drink

Total cost = $ 5.90 + 3.20 + 3.60

= $12.70 [B1]

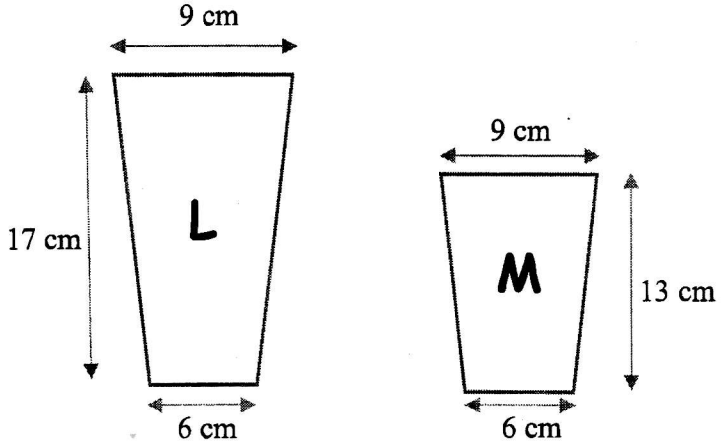
He should choose Option D to minimise his spending

[B1 – Correct Option with logical and reasonable explanation] [4]

OR He should choose Option C as for $0.20 more, he can get an extra packet of medium fries so it is the most value – for – money option.

FREE TEST PAPERS - FREETESTPAPER.COM

(b) The diagram below shows the cross-sectional area of the large (L) and medium (M) drink cups sold by the fast food restaurant in part **(a)**. The Large and Medium cups have a height of 17 cm and 13 cm respectively. The top and bottom **diameters** of both cups are 9 cm and 6 cm respectively



The volume of a cup is given by $V = \frac{1}{3}\pi h\left(R^2 + Rr + r^2\right)$ where h is the height, R and r are the radii of the top and bottom of the cup respectively. Using the information from part **(a)**, determine whether the medium cup or large cup gives better value for money.

Answer

$$V_L = \frac{1}{3}\pi(17)\left[\left(\frac{9}{2}\right)^2 + \frac{9}{2}\left(\frac{6}{2}\right) + \left(\frac{6}{2}\right)^2\right]$$
$$= 242.25\pi \text{ cm}^3 \text{ or } 761 cm^3 \,(3sf) \quad [B1]$$

$$V_M = \frac{1}{3}\pi(13)\left[\left(\frac{9}{2}\right)^2 + \frac{9}{2}\left(\frac{6}{2}\right) + \left(\frac{6}{2}\right)^2\right]$$
$$= 185.25\pi \text{ cm}^3 \text{ or } 582\text{cm}^3\,(3sf) \quad [B1]$$

For L cup:

$$\text{Volume per \$1} = \frac{357\pi}{3.60}$$
$$= 3.11541\ldots \text{ cm}^3$$
[M1 – Find cost/unit volume]

For M cup:

$$\text{Volume per \$} = \frac{273\pi}{2.80}$$
$$= 306.305\, cm^3$$

$\therefore$ Large cup gives more value for money [A1]

OR

$$\frac{\text{Price of L}}{\text{Price of M}} = \frac{P_L}{P_M} = \frac{3.6}{2.8} = \frac{9}{7}$$
$$\frac{V_L}{V_M} = \frac{17}{13}$$

By comparing ratio:

$$\frac{P_L}{P_M} = \frac{9}{7} \times \frac{13}{13} = \frac{117}{91} \quad [\text{M1} - \text{Comparing ratio}]$$
$$\frac{V_L}{V_M} = \frac{17}{13} \times \frac{7}{7} = \frac{119}{91}$$

Since $\frac{V_L}{V_M} > \frac{P_L}{P_M}$,

buying a Large drink gives more value for money.
[A1 – Conclusion]

FREE TEST PAPERS - FREETESTPAPER.COM

BLANK PAGE

FREE TEST PAPERS - FREETESTPAPER.COM